

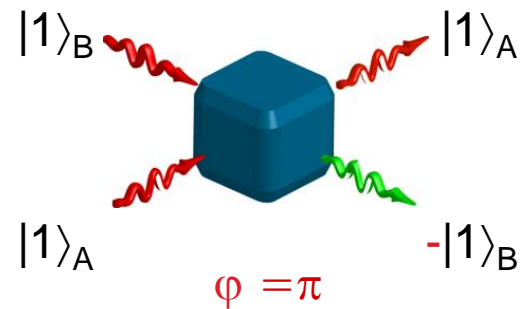
# Quantum optics with an intracavity Rydberg gas

Alexei Ourjoumtsev

Erwan Bimbard, Rajiv Boddeda, Nicolas Vitrant, Andrey Grankin, Valentina Parigi, Jovica Stanojevic, Imam Usmani, Etienne Brion, Philippe Grangier

Institut d'Optique, Palaiseau, France

# Photonic interactions

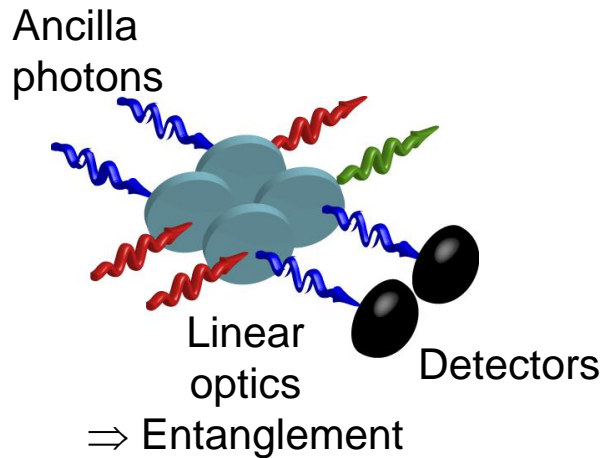


Example: photon A shifts phase of photon B

Classical non-linear media:  $\varphi < 10^{-6}$  before photons are lost

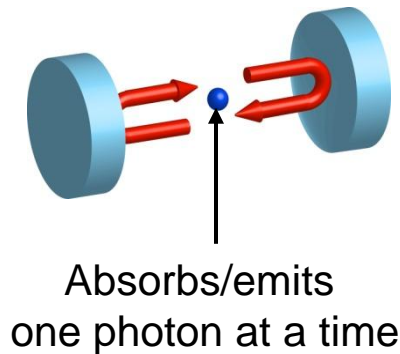
# « Established » methods

## Projective measurements

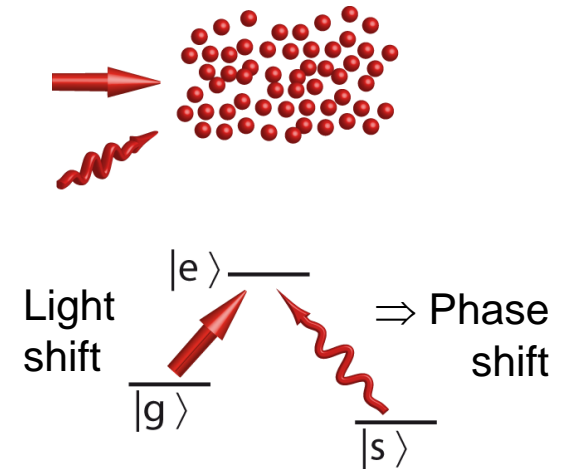


## Cavity QED

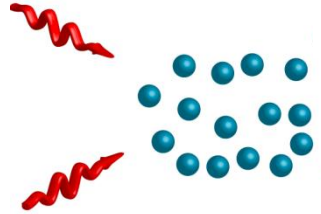
2-level « atom »  
+ high-finesse cavity



## Dense atomic ensembles



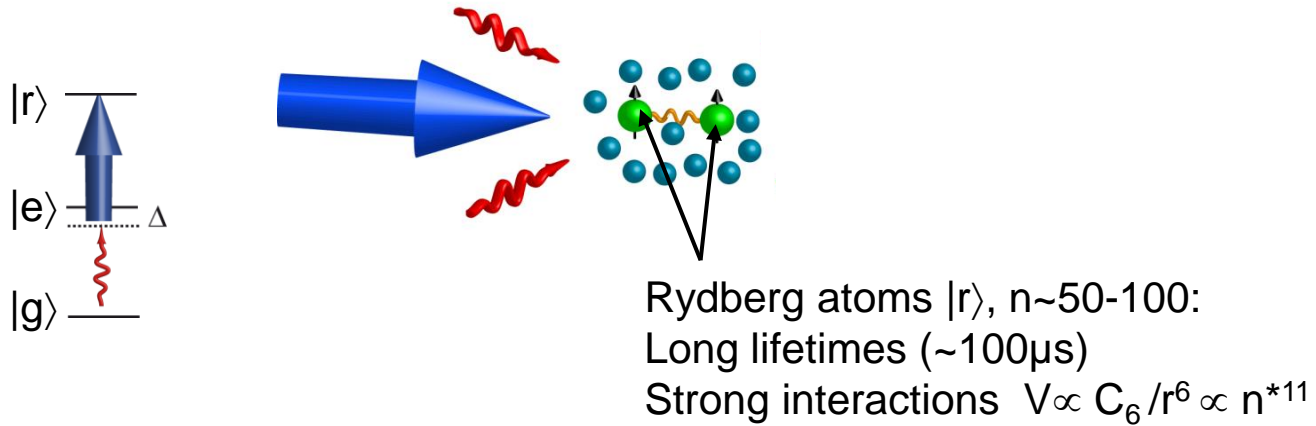
# Our approach



Injected in  
a cold gas

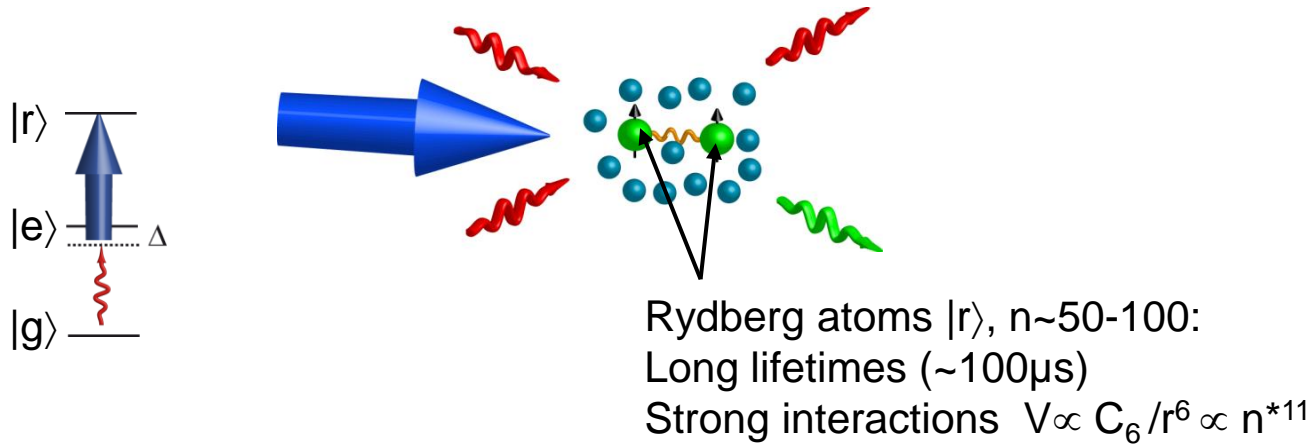
Photons:

# Our approach



Photons:  
Injected in a cold gas  $\rightarrow$  Interact via Rydberg excitations

# Our approach

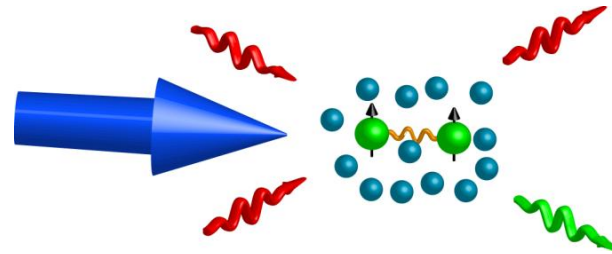


Photons:  
Injected in a cold gas  $\rightarrow$  Interact via Rydberg excitations  $\rightarrow$  Retrieved in desired mode

# Outline

Atomic physics:  
create  
non-linear effects

**Part I**



Quantum optics:  
Manipulate & detect  
quantum states

**Part II**

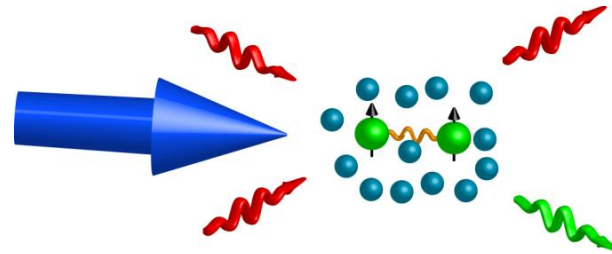
Rydberg-mediated  
photonic interactions

**Part III**

# Outline

Atomic physics:  
create  
non-linear effects

**Part I**



Quantum optics:  
Manipulate & detect  
quantum states

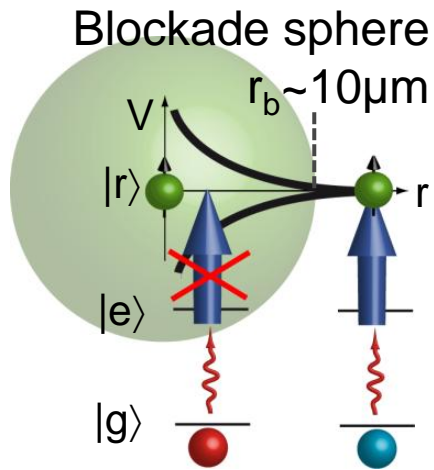
**Part II**

Rydberg-mediated  
photonic interactions

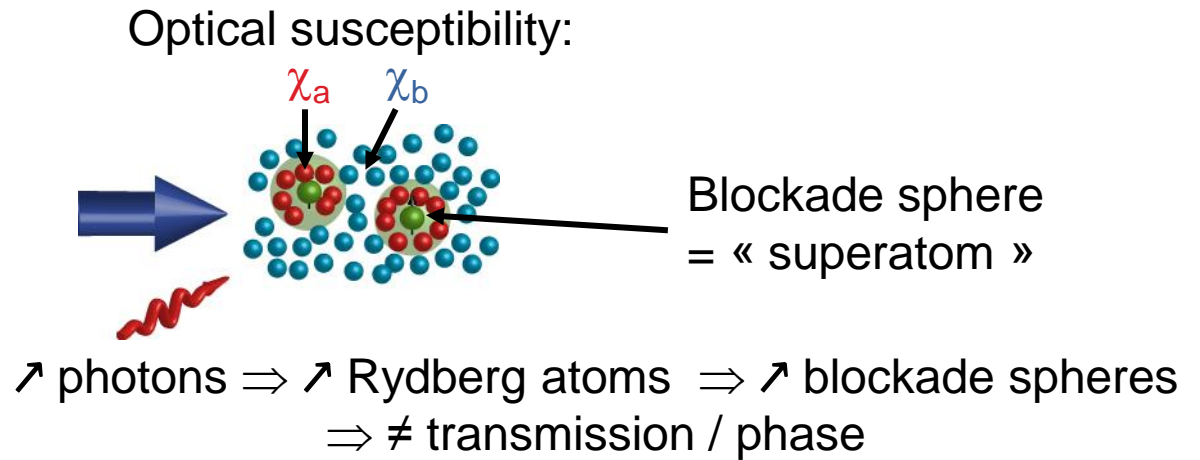
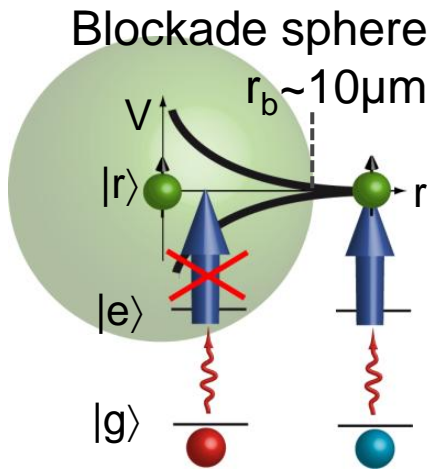
**Part III**



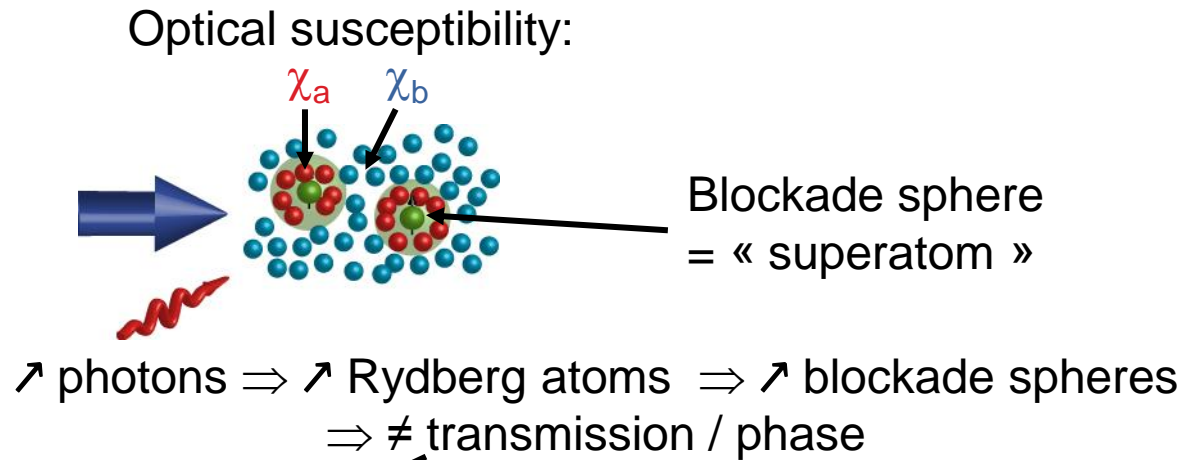
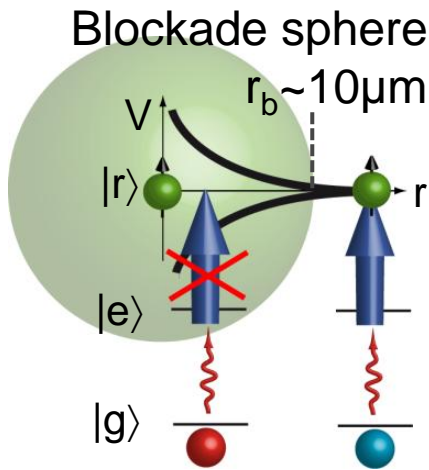
# Rydberg blockade



# Rydberg blockade

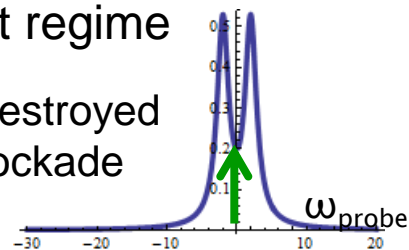


# Rydberg blockade



Resonant regime

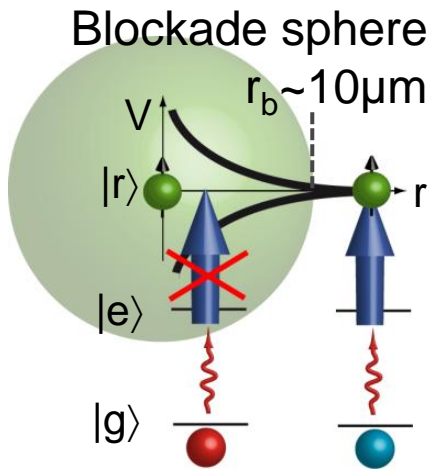
EIT destroyed  
by blockade



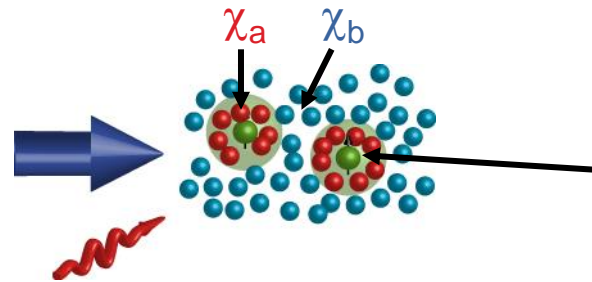
Pritchard *&al*, PRL **105**, 193603 (2010)

Ates *&al*, PRA **83**, 041802(R) (2011)

# Rydberg blockade



Optical susceptibility:

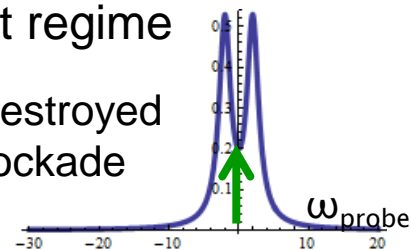


Blockade sphere  
= « superatom »

$\nearrow$  photons  $\Rightarrow$   $\nearrow$  Rydberg atoms  $\Rightarrow$   $\nearrow$  blockade spheres  
 $\Rightarrow \neq$  transmission / phase

Resonant regime

EIT destroyed  
by blockade

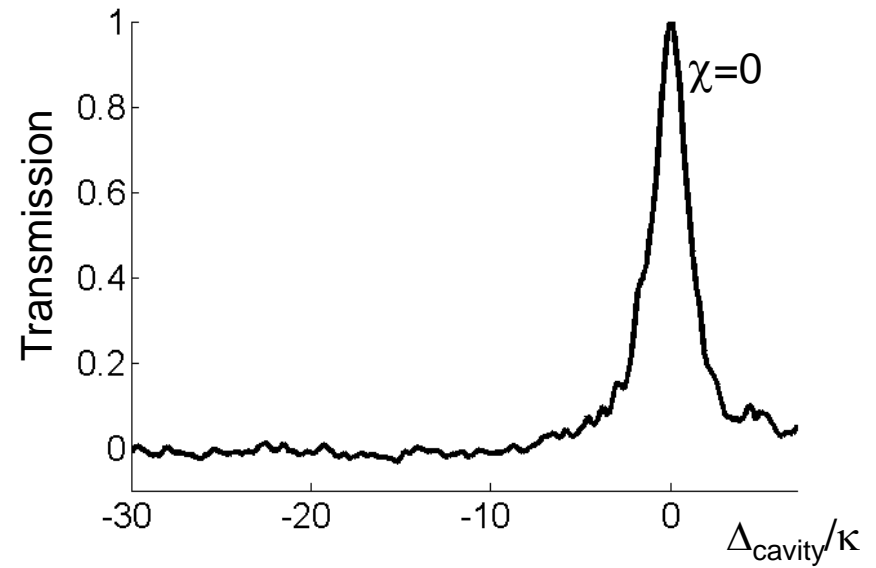
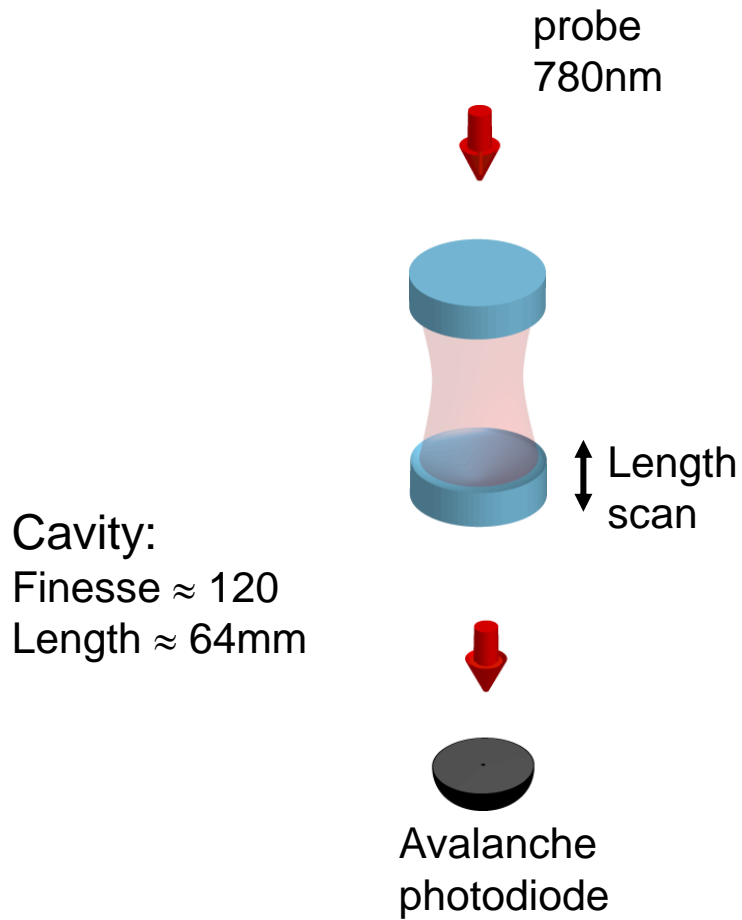


Off-resonant regime?

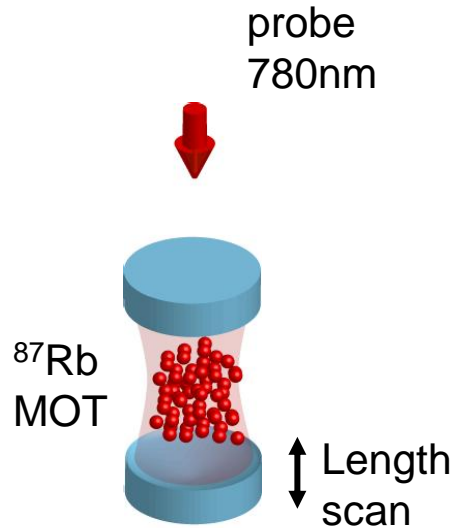
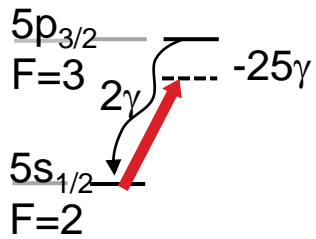
Pritchard *&al*, PRL **105**, 193603 (2010)

Ates *&al*, PRA **83**, 041802(R) (2011)

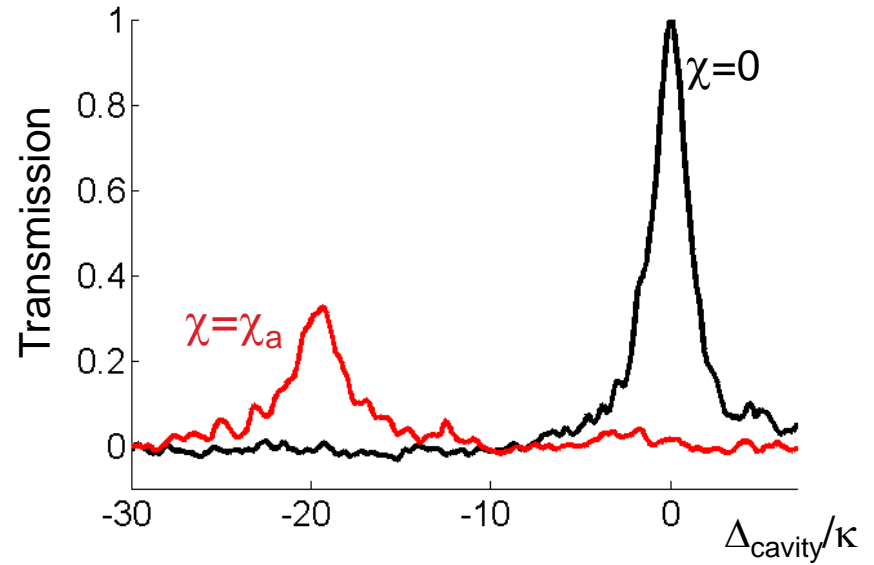
# Dispersion measurement



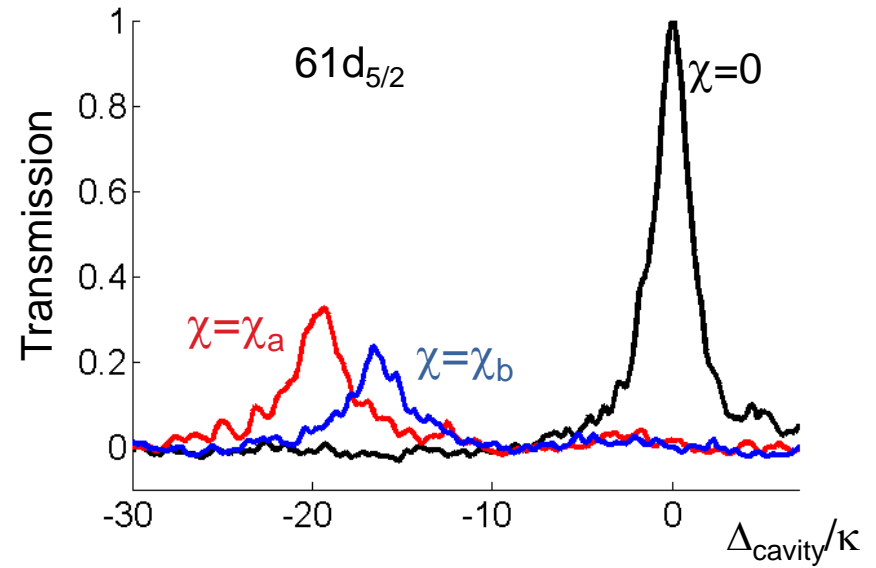
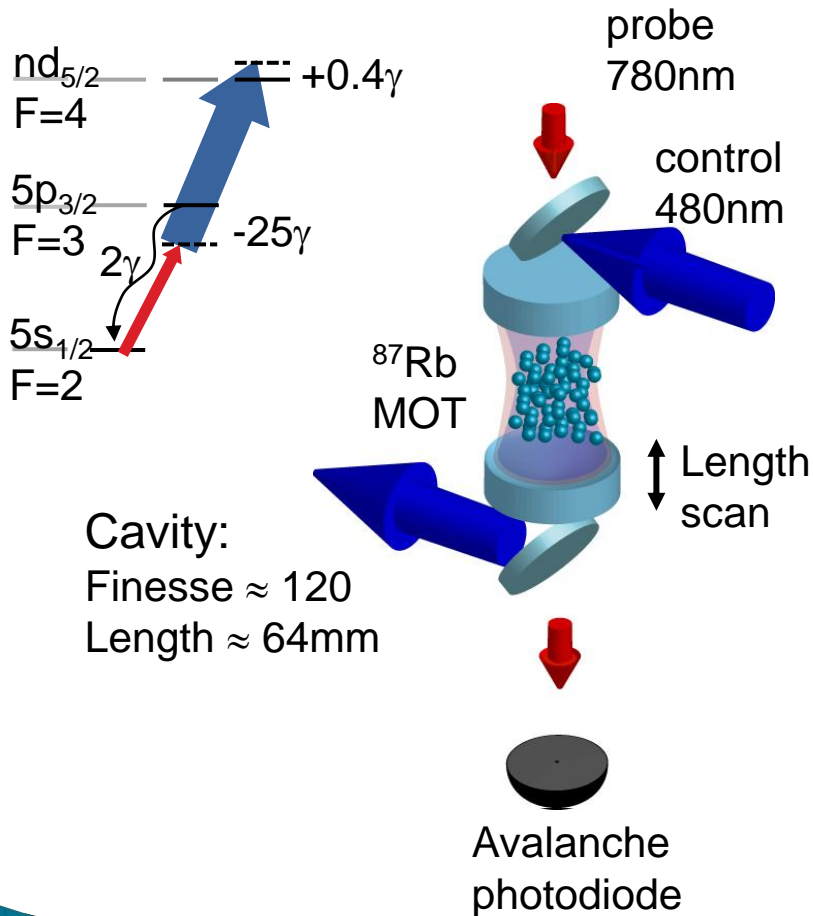
# Dispersion measurement



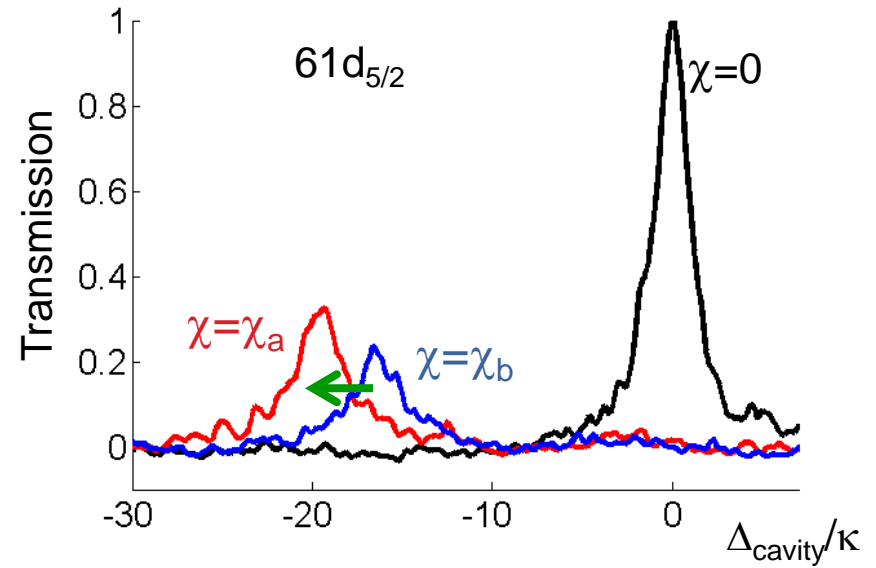
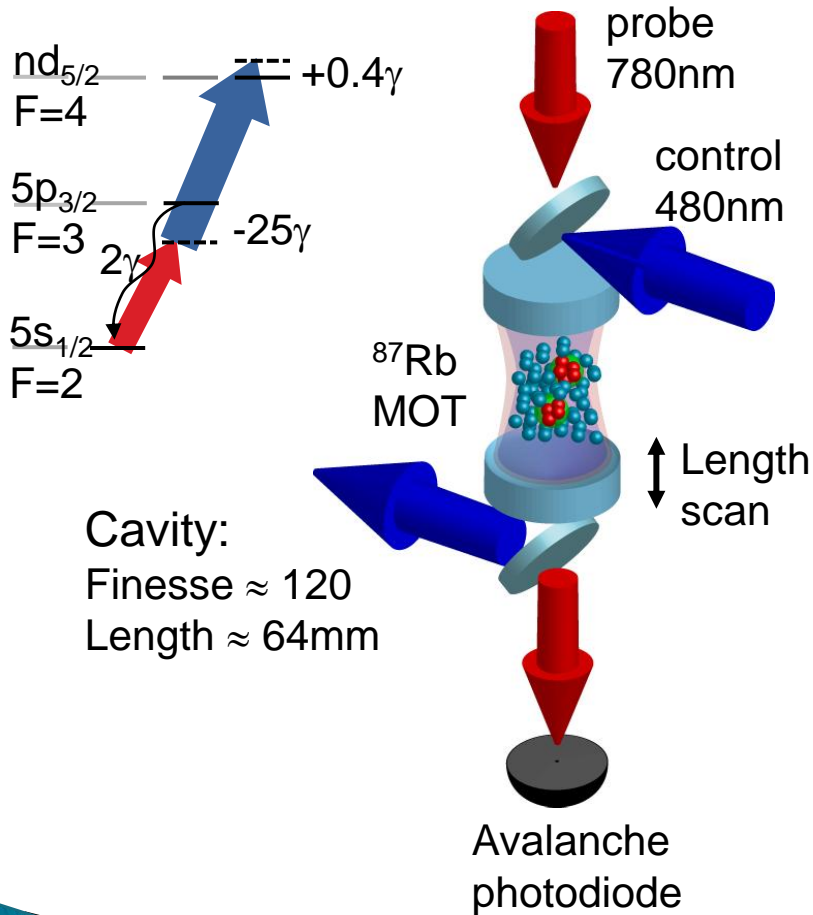
Cavity:  
Finesse  $\approx 120$   
Length  $\approx 64\text{mm}$



# Dispersion measurement



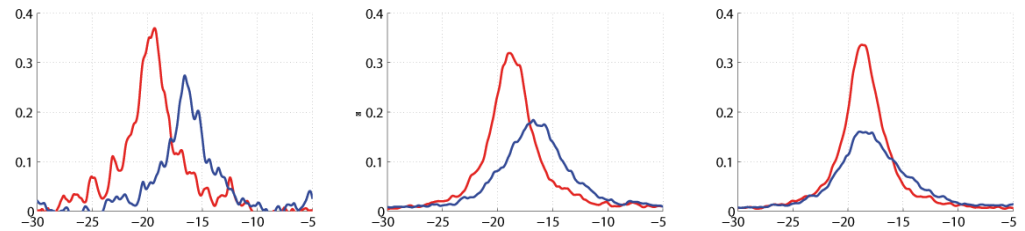
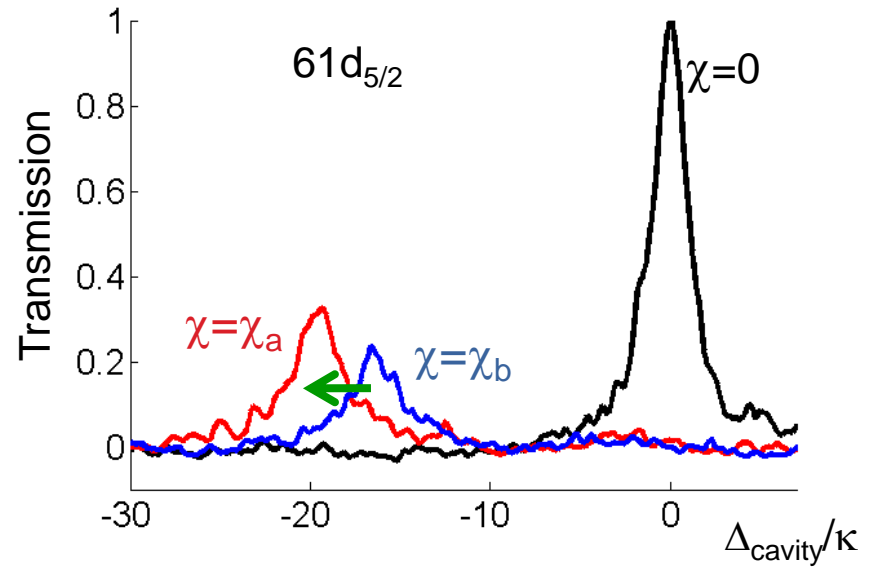
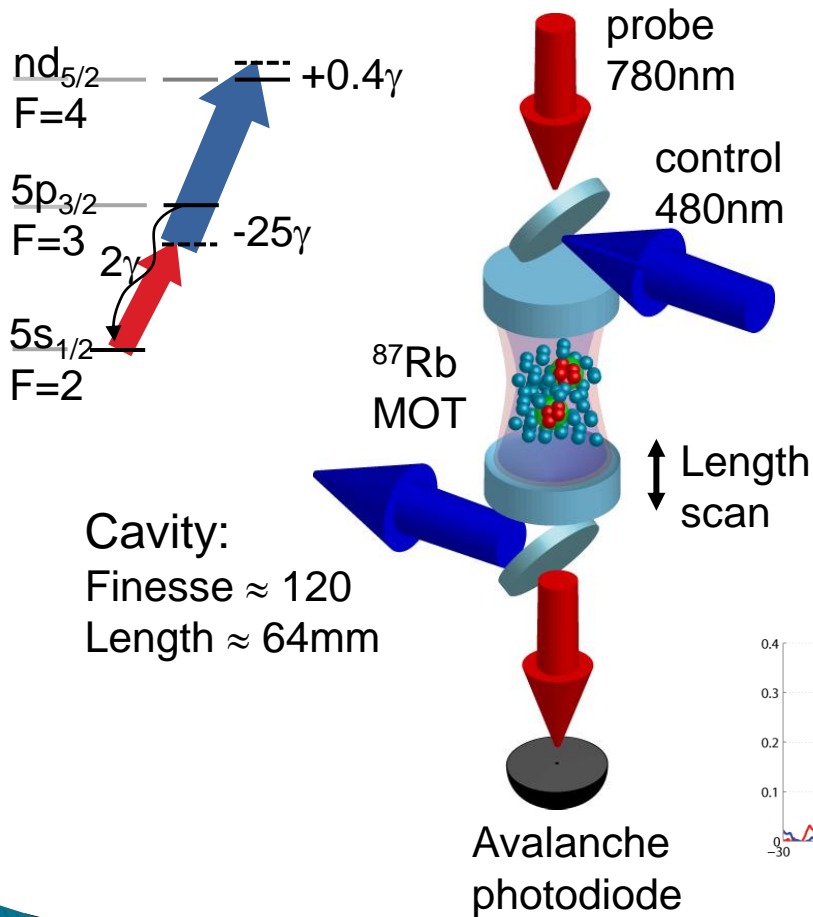
# Dispersion measurement



Expected bistability... saw ions  
 $\Rightarrow$  weaker driving, faster scan.

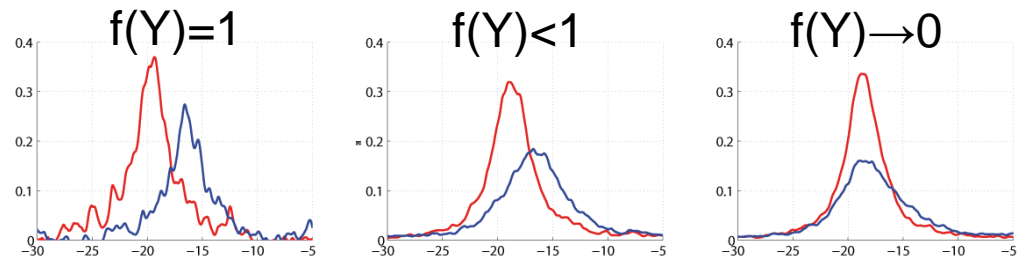
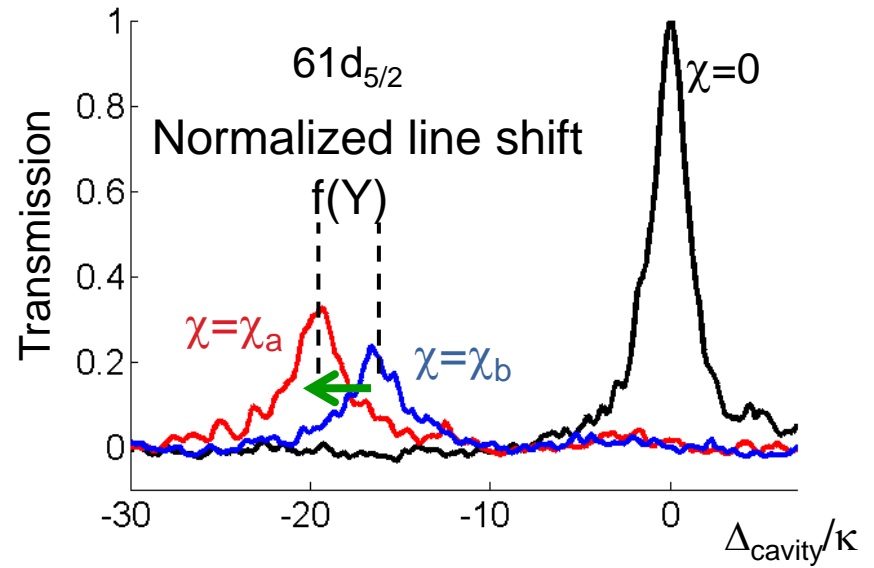
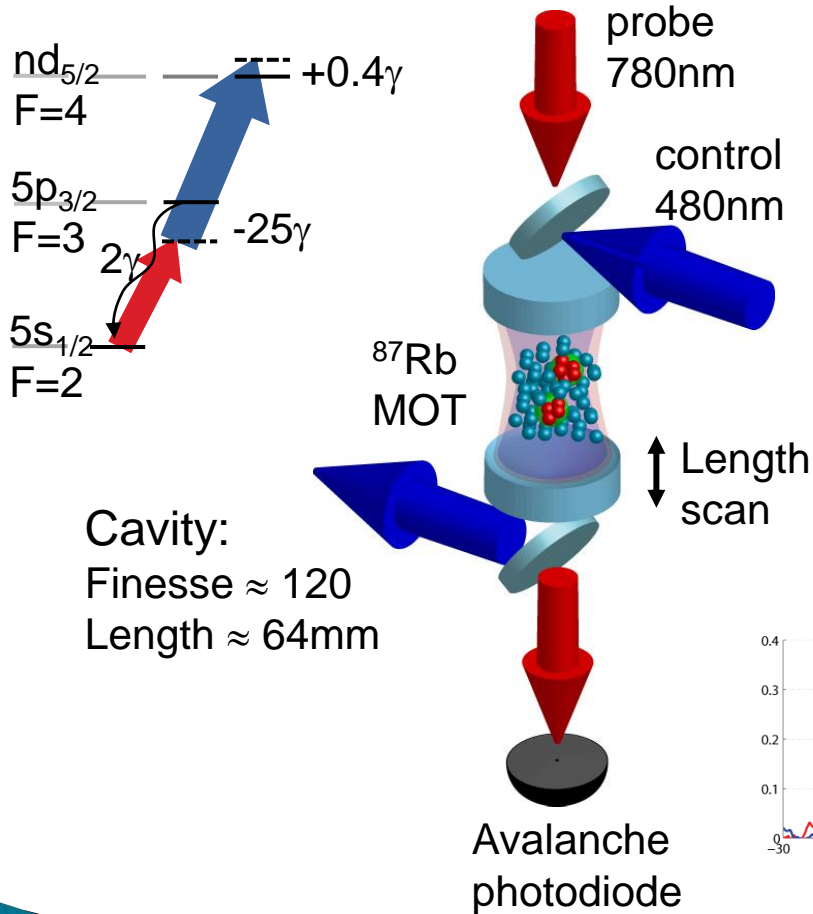


# Dispersion measurement



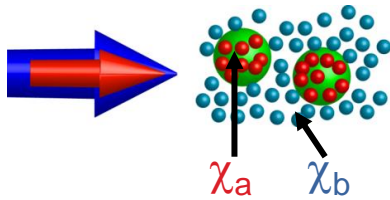
Increasing probe power  $Y=P/P_{\text{sat}}$

# Dispersion measurement



Increasing probe power  $Y = P/P_{\text{sat}}$

# Dispersion measurement



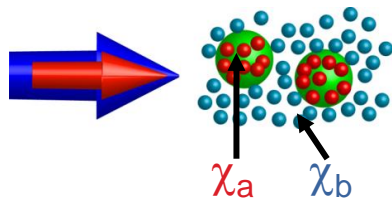
Normalized line shift  $f(Y)$ :

$$\frac{df}{dY}(0) \propto n_{\text{block}} = \rho V_{\text{sphere}}$$

Atomic  
density

Volume of a blockade sphere  
 $\propto \sqrt{C_6} \propto (n^*)^{5.5}$

# Dispersion measurement

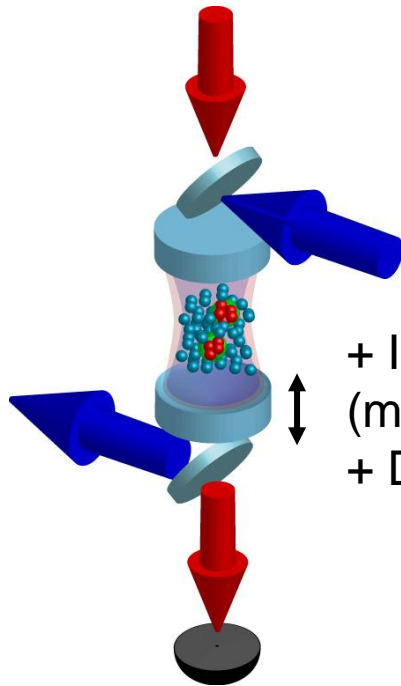


Normalized line shift  $f(Y)$ :

$$\frac{df}{dY}(0) \propto n_{\text{block}} = \rho V_{\text{sphere}}$$

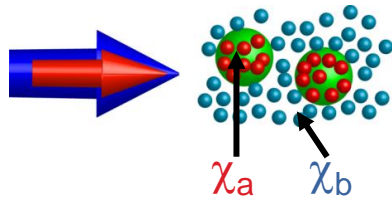
Atomic  
density

Volume of a blockade sphere  
 $\propto \sqrt{C_6} \propto (n^*)^{5.5}$



- + Inhomogeneous beams  
(mismatched standing waves & transverse profiles)
- + Dynamics

# Dispersion measurement

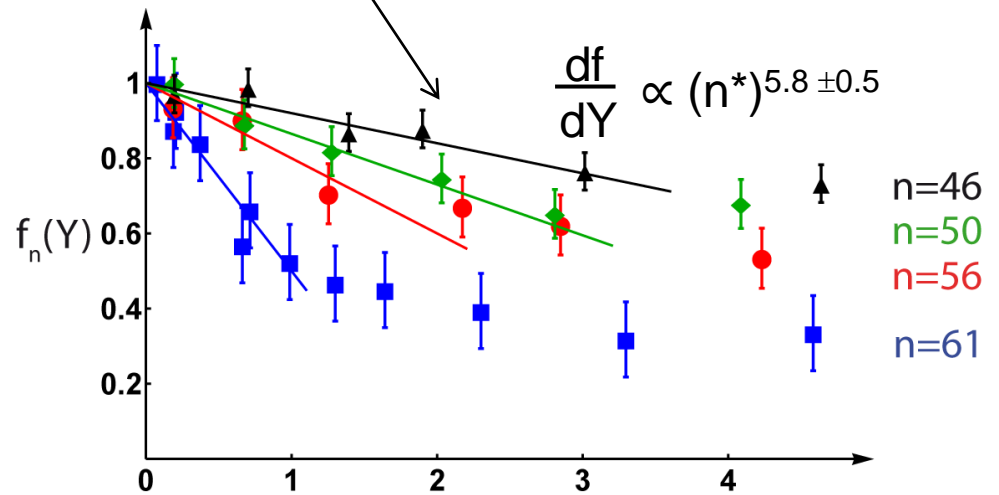
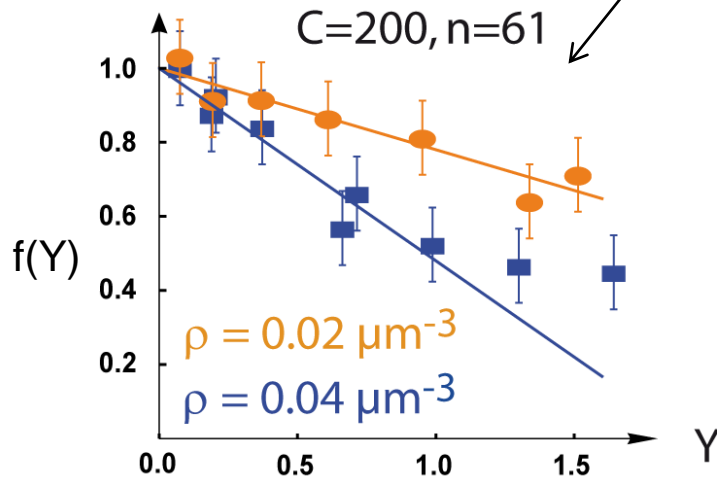


Normalized line shift  $f(Y)$ :

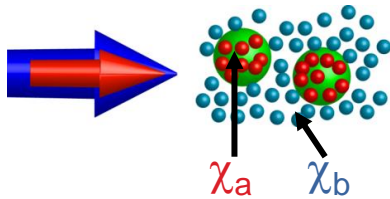
$$\frac{df}{dY}(0) \propto n_{\text{block}} = \rho V_{\text{sphere}} \quad (+ \text{inhomogeneities \& dynamics})$$

Atomic density

Volume of a blockade sphere  
 $\propto \sqrt{C_6} \propto (n^*)^{5.5}$



# Blockade model validity

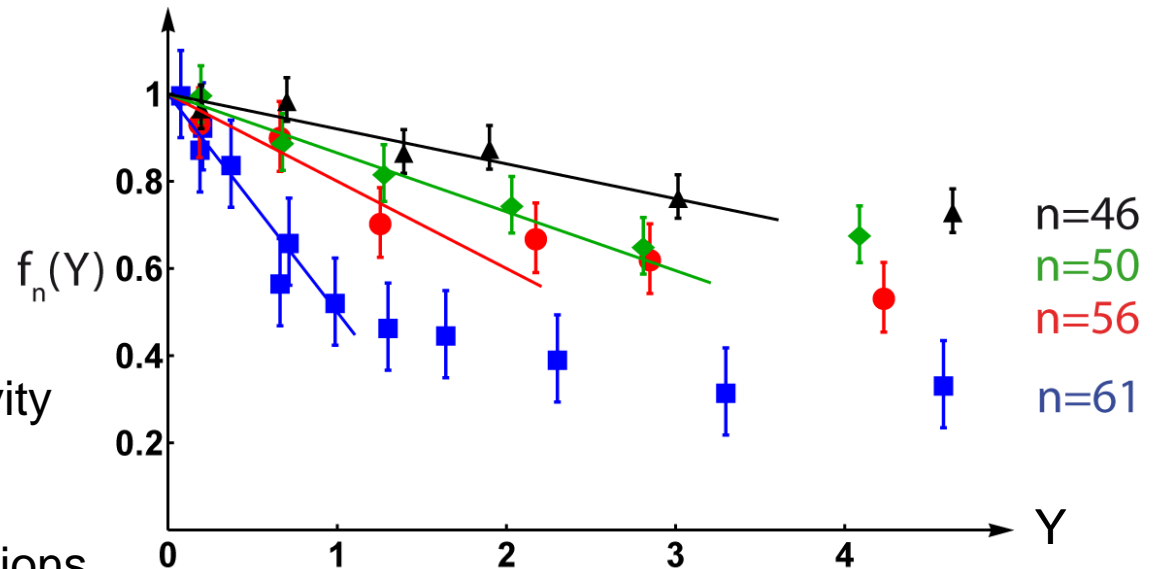


Low-power  $\chi^{(3)}$  regime ( $Y \ll 1$ ):

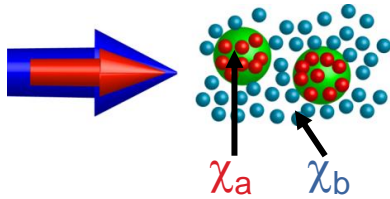
$$\chi \approx \chi_b + (\chi_a - \chi_b) sX$$

$\swarrow$        $\swarrow$        $\swarrow$        $\swarrow$   
 Intracavity power

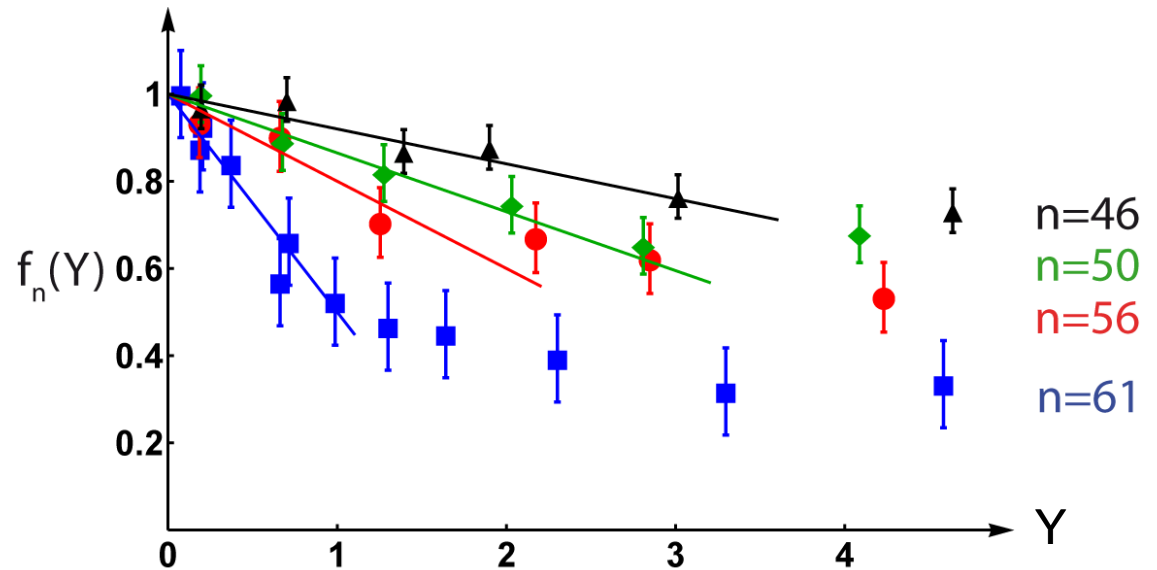
3-level optical Bloch equations  
 (lowest-order expansion)  
 + spatial inhomogeneities  
 + dynamics



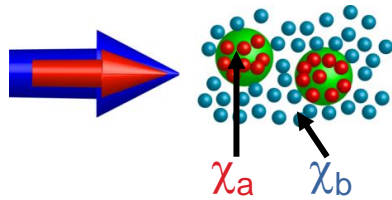
# Blockade model validity



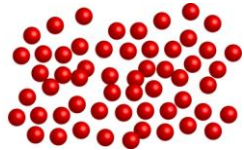
Saturated regime ?



# Blockade model validity

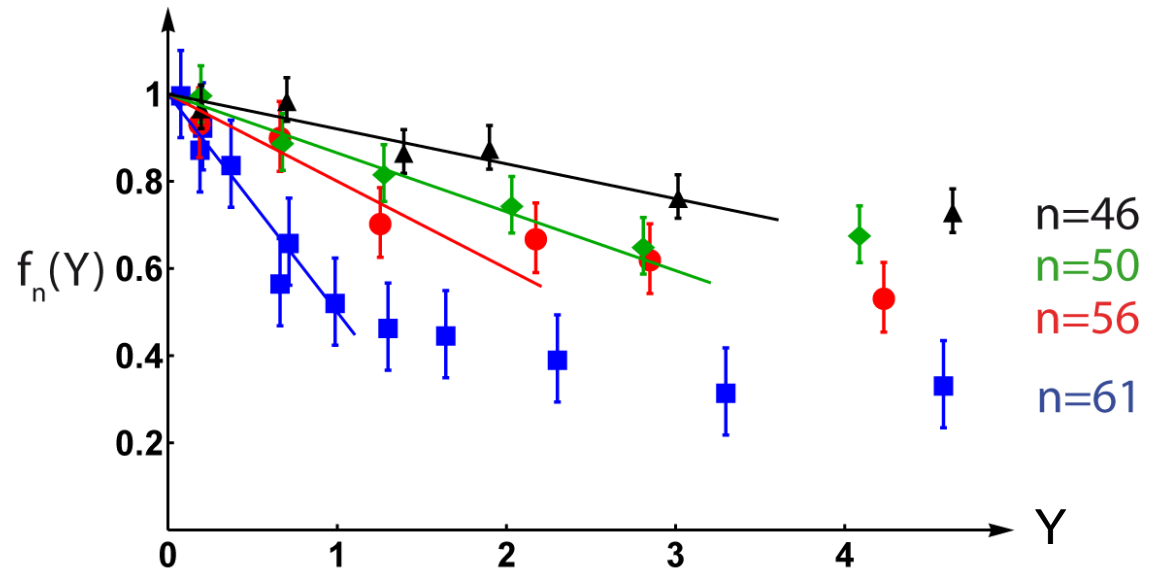


2-level atoms



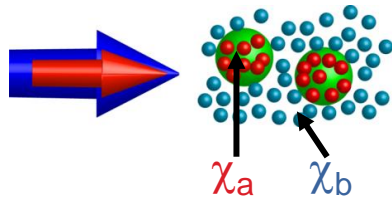
$$\chi = \frac{\chi^{(1)}}{1+sX}$$

Saturated regime ?

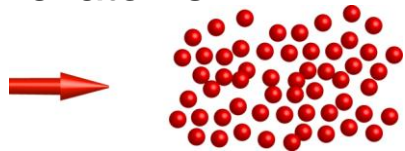




# Blockade model validity

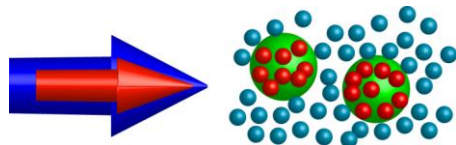


2-level atoms



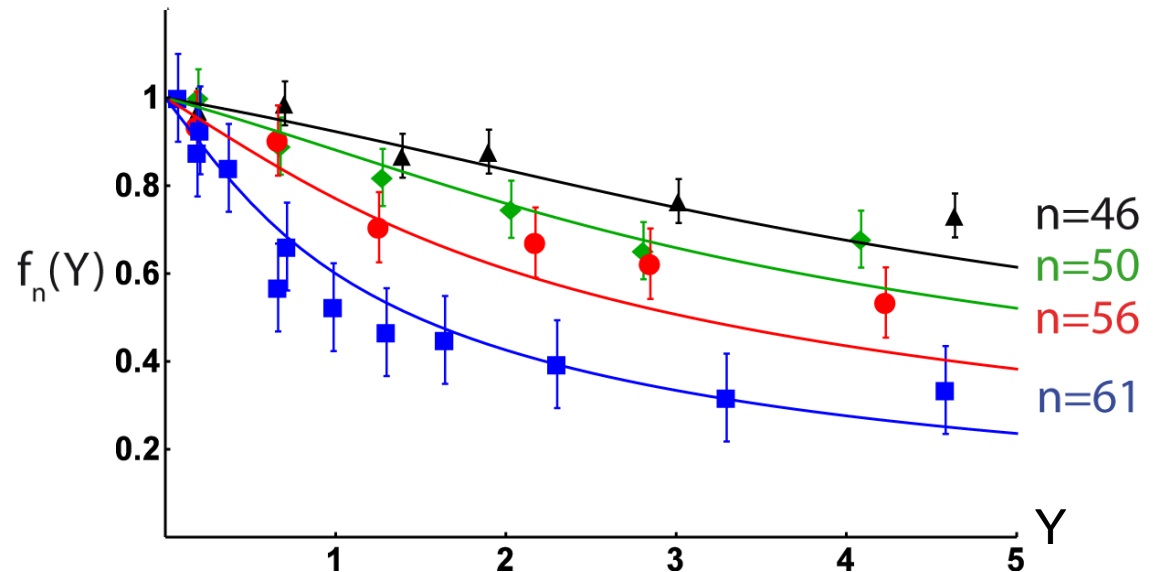
$$\chi = \frac{\chi^{(1)}}{1+sX}$$

Rydberg « superatoms »



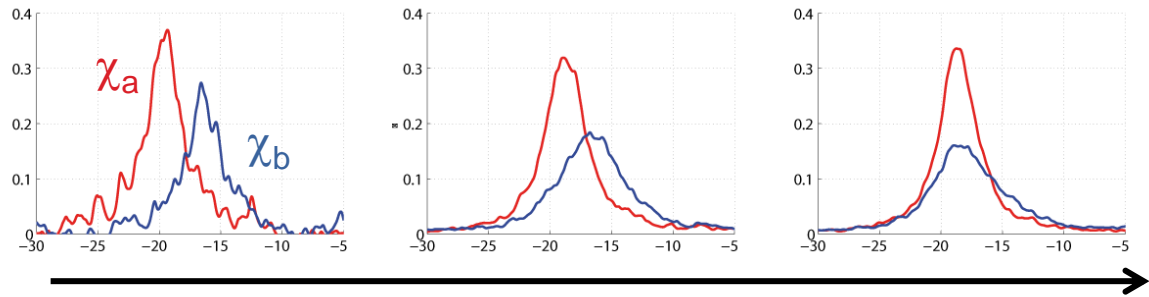
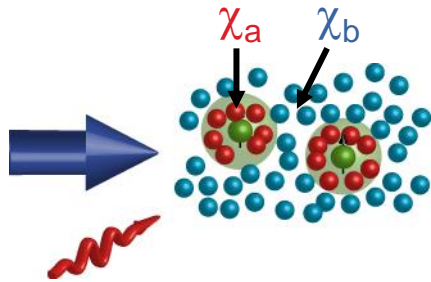
$$\chi - \chi_a = \frac{\chi_b - \chi_a}{1+sX}$$

Saturated regime ?



Bloch equations + inhomogeneities + dynamics

# Blockade model validity

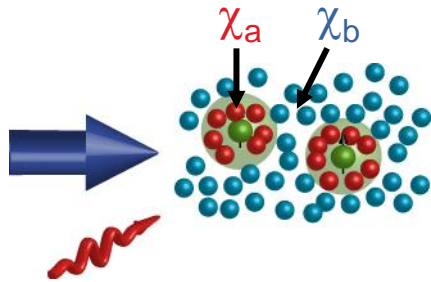


Increasing probe power  $Y=P/P_{\text{sat}}$

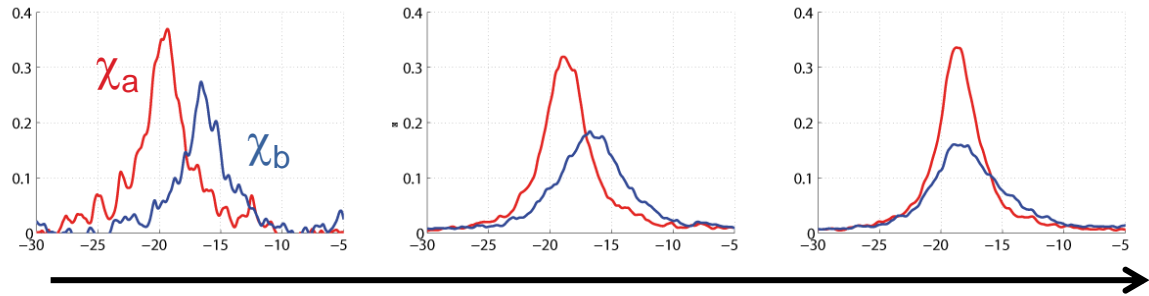
Dispersion  $\propto \text{Re}(\chi)$  : OK

Absorption  $\propto \text{Im}(\chi)$  : Additional losses

# Blockade model validity



~~Hard-core  
Isotropic~~

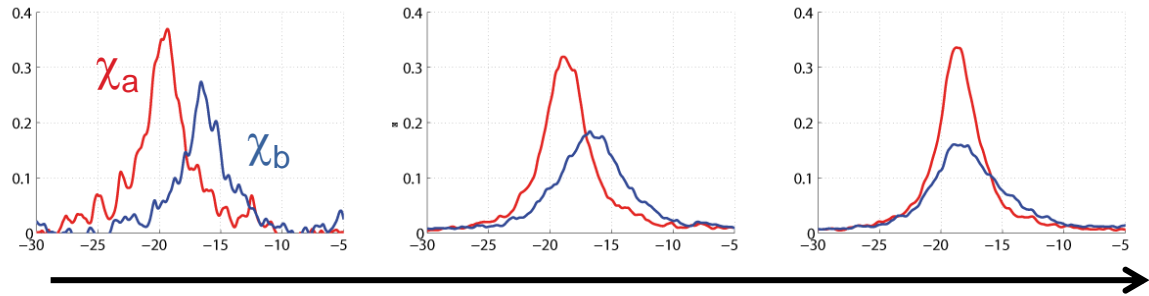
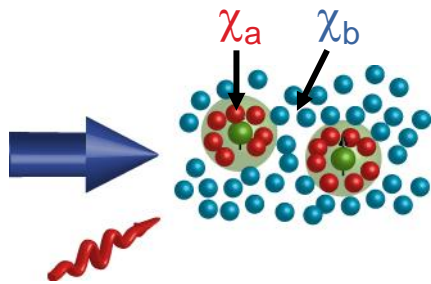


Increasing probe power  $Y = P/P_{\text{sat}}$

Dispersion  $\propto \text{Re}(\chi)$  : OK

Absorption  $\propto \text{Im}(\chi)$  : Additional losses

# Blockade model validity

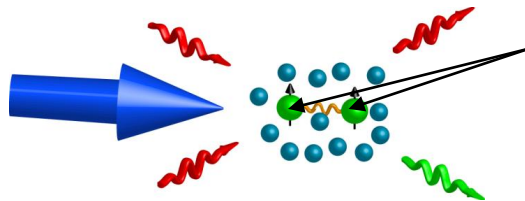


Increasing probe power  $Y=P/P_{\text{sat}}$

~~Hard-core  
Isotropic~~

Dispersion  $\propto \text{Re}(\chi)$  : OK

Absorption  $\propto \text{Im}(\chi)$  : Additional losses

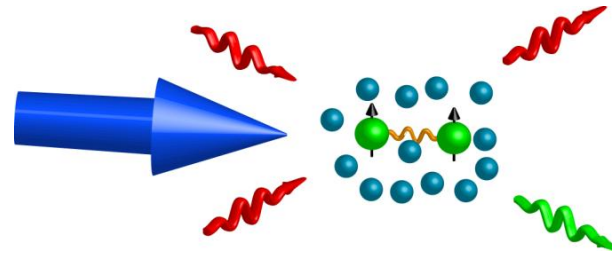


- Phase shift  $\varphi(t)=t \cdot C_6/r^6$   
 $r$  random  $\Rightarrow$  dephasing  
 Dudin & Kuzmich, Science **336**, 887 (2012)
- d states  $\Rightarrow$  angular dependence  $\Rightarrow$  dephasing

# Outline

Atomic physics:  
create  
non-linear effects

**Part I**



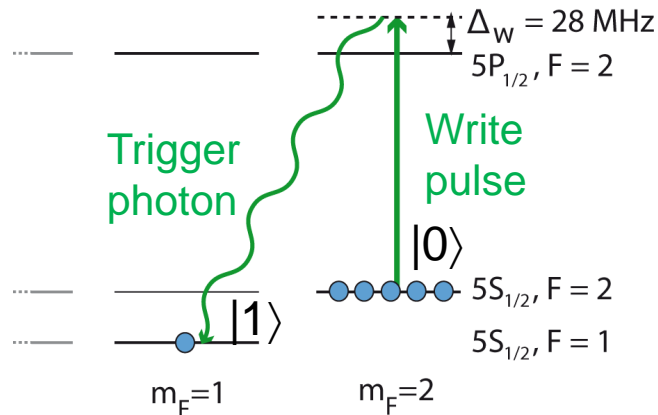
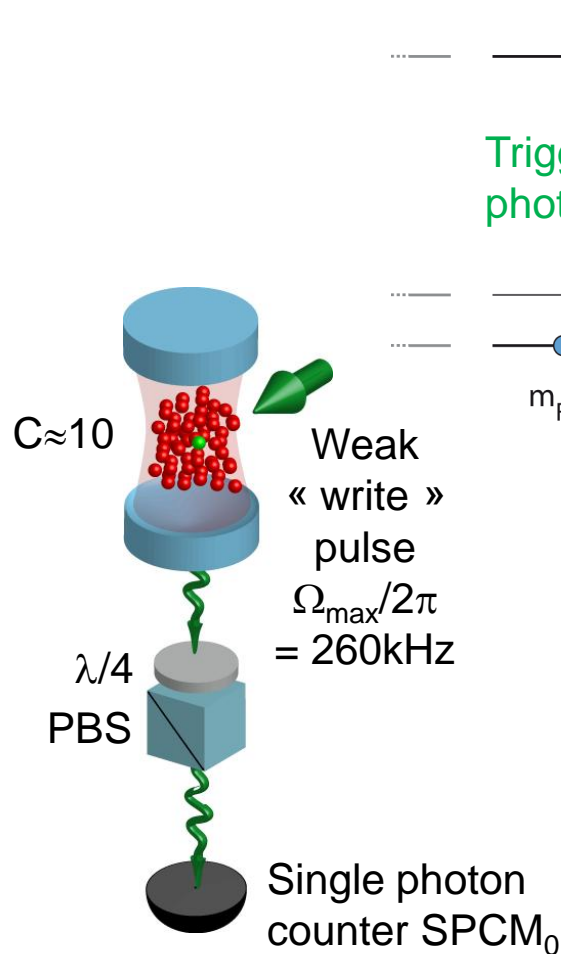
Quantum optics:  
Manipulate & detect  
quantum states

**Part II**

Rydberg-mediated  
photonic interactions

**Part III**

# Single photon source (DLCZ)



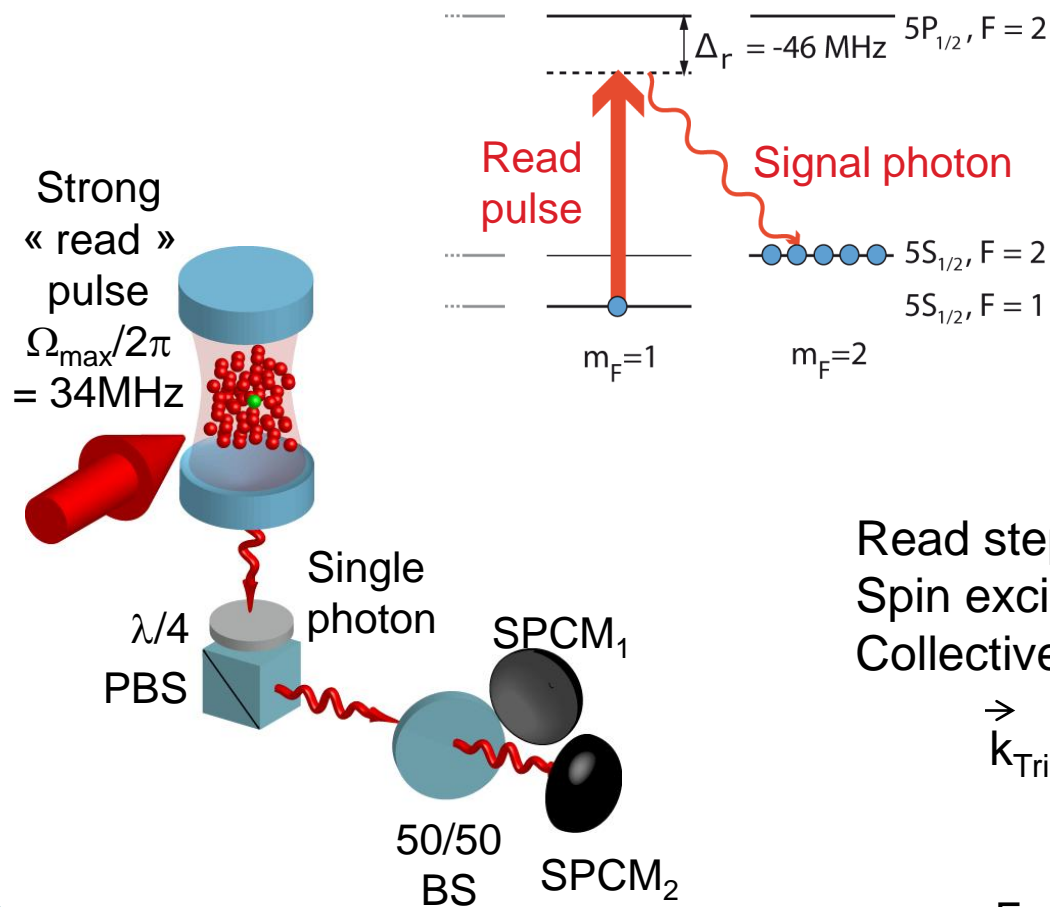
Write step:

Creates a single collective excitation

$$e^{i(\vec{k}_T - \vec{k}_W) \cdot \vec{r}_1} |100\dots 0\rangle + e^{i(\vec{k}_T - \vec{k}_W) \cdot \vec{r}_2} |010\dots 0\rangle + \dots$$

Trigger probability  $\sim 1/1000$  (rate  $\sim 100/\text{s}$ )

# Single photon source (DLCZ)

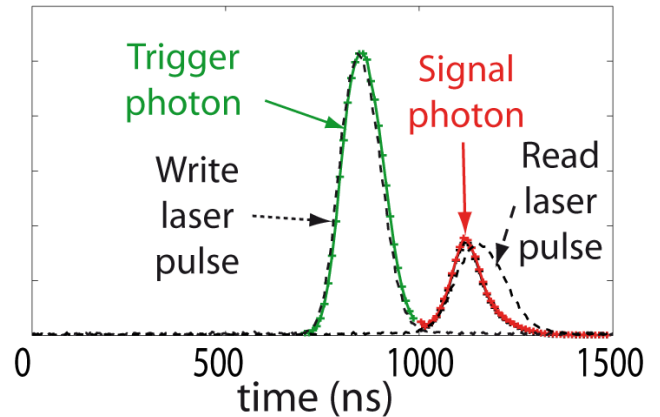
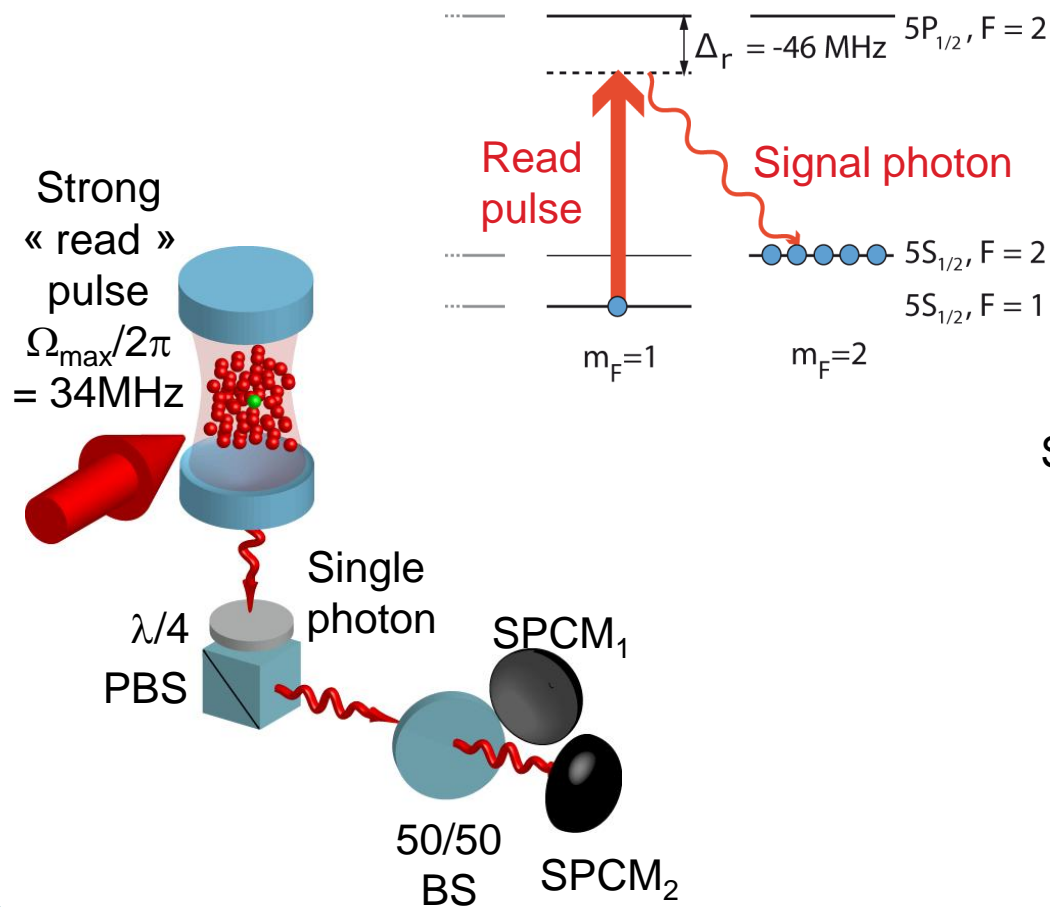


Read step:  
Spin excitation retrieved as a photon  
Collective phase-matched process

$$\vec{k}_{\text{Trigger}} - \vec{k}_{\text{Read}} = \vec{k}_{\text{Signal}} - \vec{k}_{\text{Write}}$$

Emitted in (another) cavity mode

# Single photon source (DLCZ)

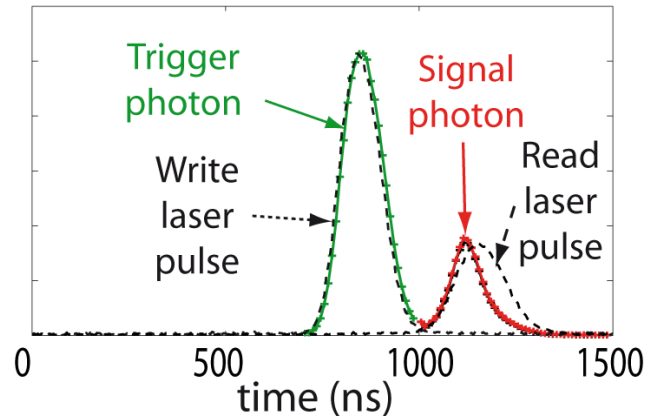
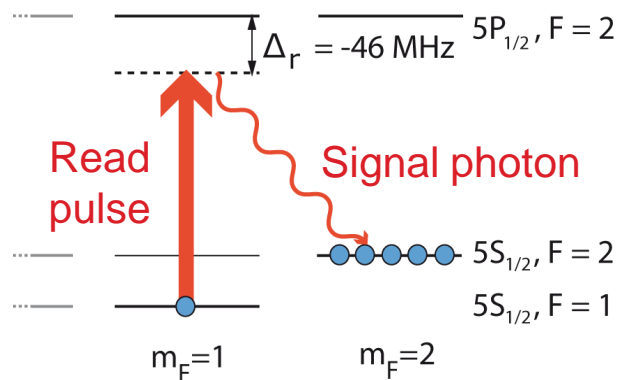
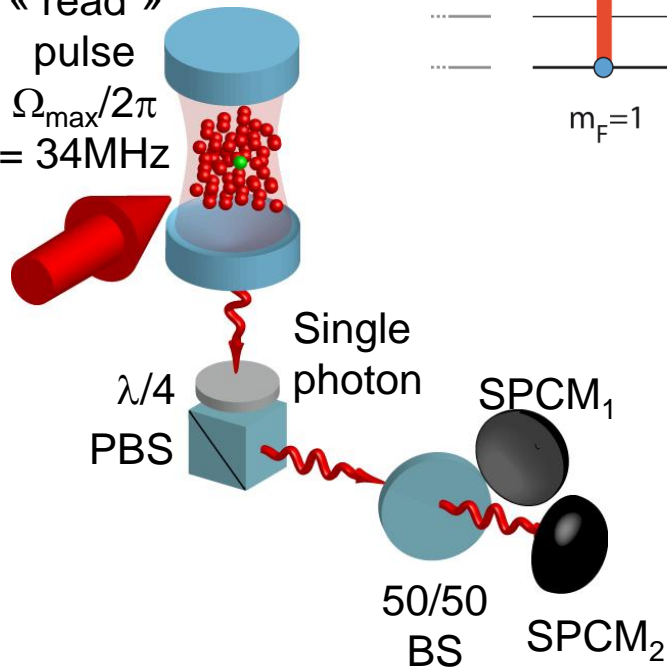


Stanojevic *et al*, PRA **84**, 053830 (2011)



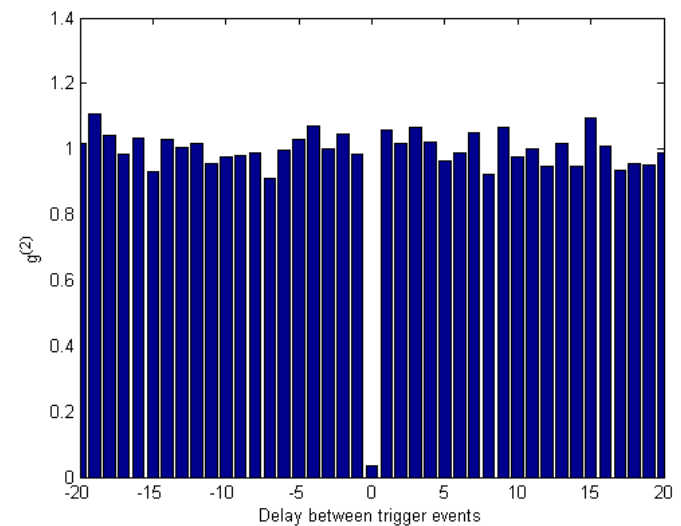
# Single photon source (DLCZ)

Strong  
« read »  
pulse  
 $\Omega_{\max}/2\pi$   
= 34MHz



Stanojevic *et al*, PRA **84**, 053830 (2011)

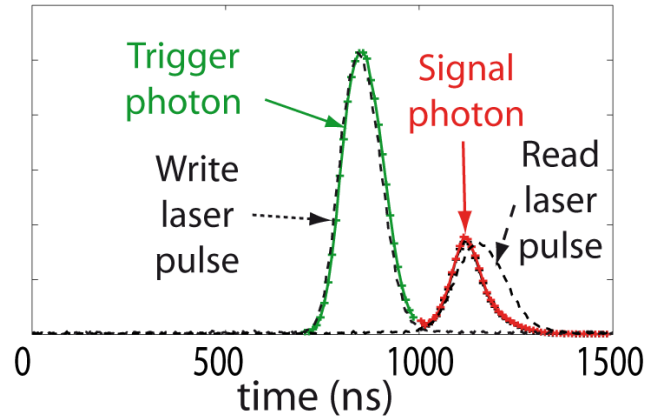
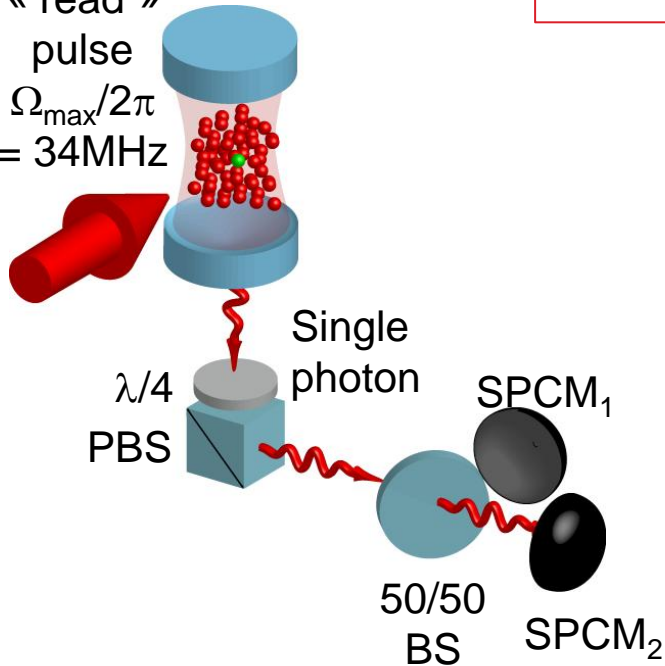
$$g^{(2)}(0) = \frac{\langle \hat{a}^\dagger \hat{a}^\dagger \hat{a} \hat{a} \rangle}{\langle \hat{a}^\dagger \hat{a} \rangle^2} = 0.03$$



# Single photon source (DLCZ)

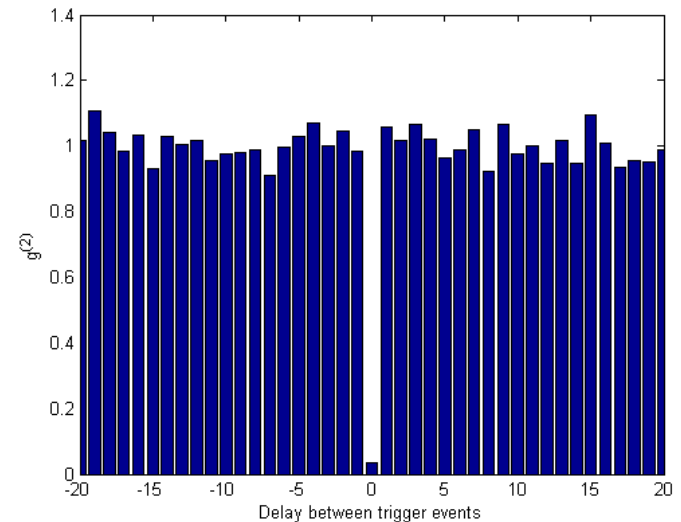
Frequency ?  
Chirp?  
Spectral width?  
...

Strong  
« read »  
pulse  
 $\Omega_{\max}/2\pi$   
= 34MHz



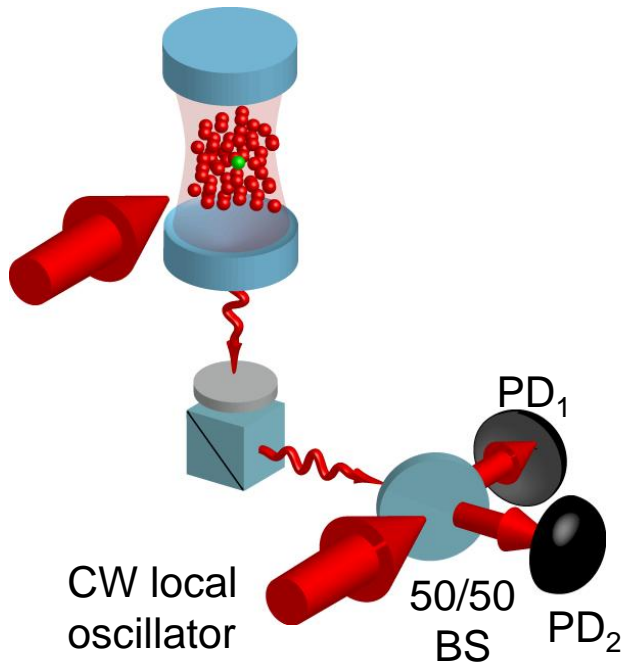
Stanojevic *et al*, PRA **84**, 053830 (2011)

$$g^{(2)}(0) = \frac{\langle \hat{a}^\dagger \hat{a}^\dagger \hat{a} \hat{a} \rangle}{\langle \hat{a}^\dagger \hat{a} \rangle^2} = 0.03$$



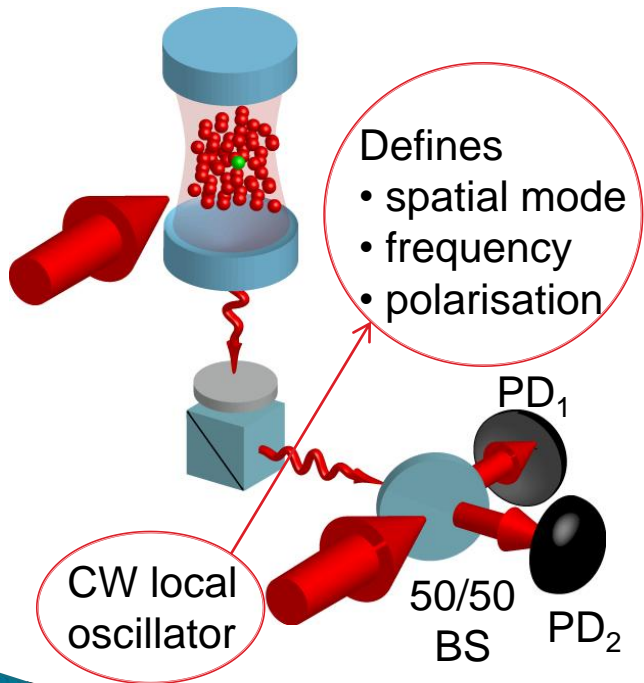
# Homodyne tomography

$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$



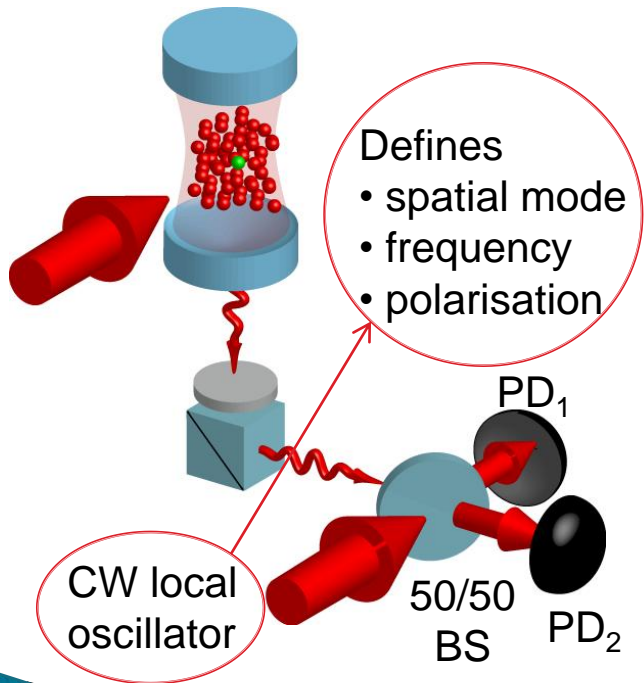
# Homodyne tomography

$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$

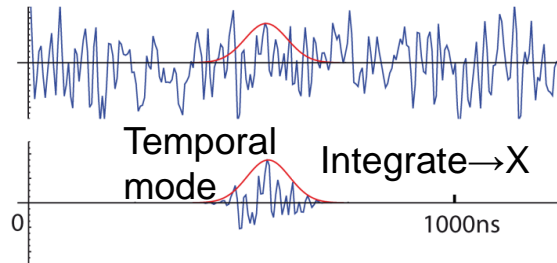


# Homodyne tomography

$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$

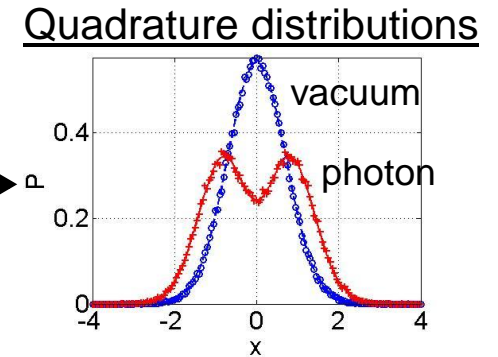
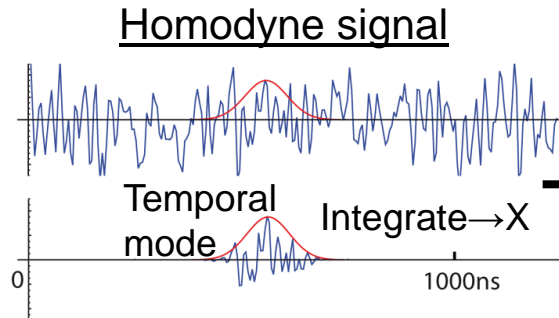
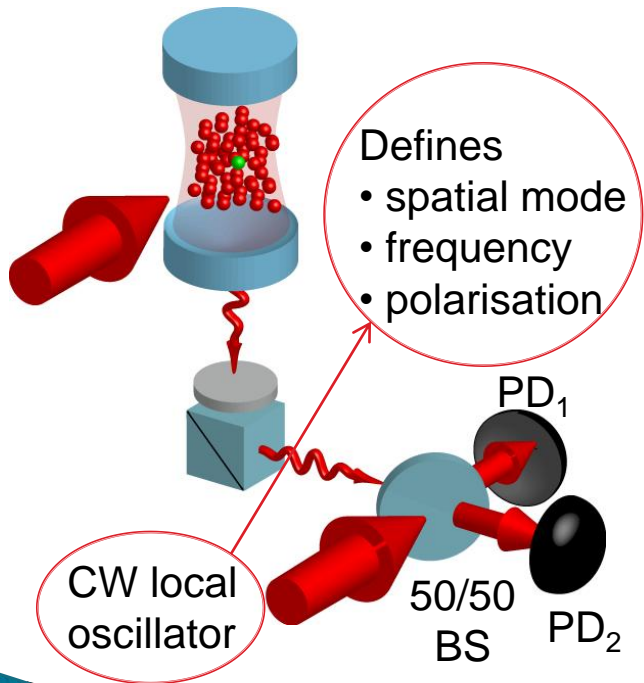


## Homodyne signal



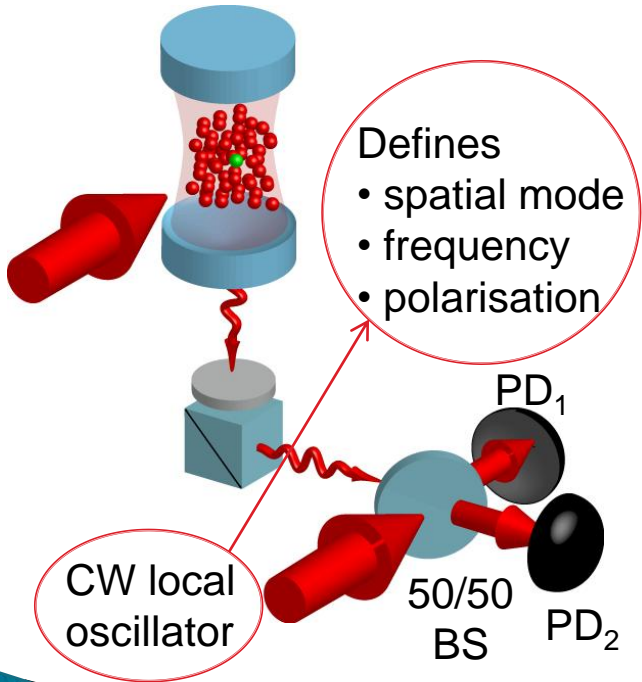
# Homodyne tomography

$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$

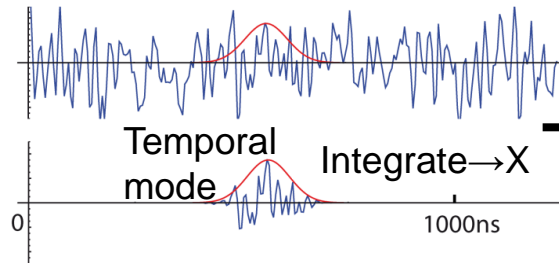


# Homodyne tomography

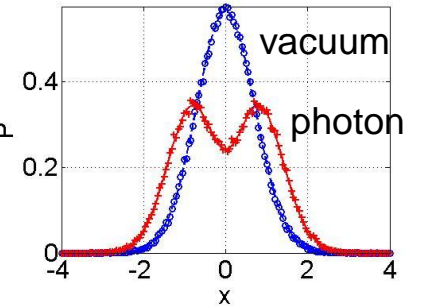
$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$



## Homodyne signal



## Quadrature distributions

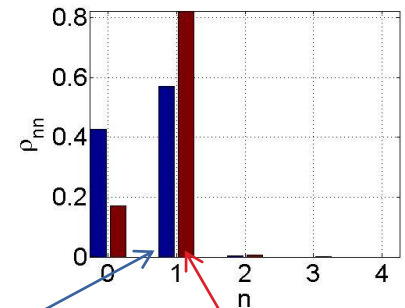


↓ maximal likelihood

## Detector's efficiency:

- optical = 92%
- mode-matching = 97%
- quantum = 91%
- + Electronic noise = 1%

## Density matrix

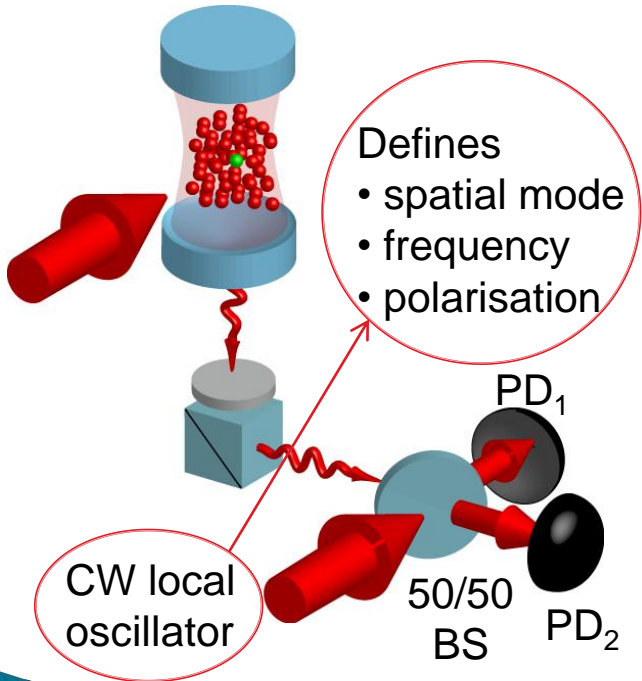


measured state: 57%

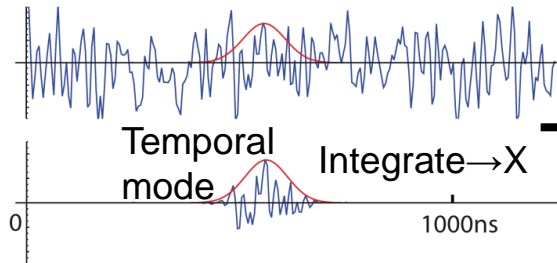
generated state: 82%

# Homodyne tomography

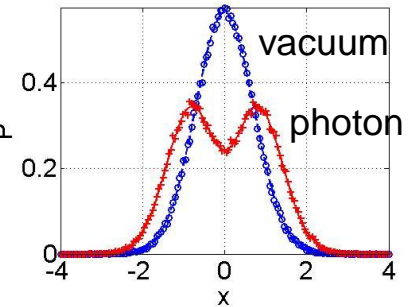
$$I_1 - I_2 \propto X = \frac{\hat{a}e^{-i\varphi} + \hat{a}^\dagger e^{i\varphi}}{\sqrt{2}}$$



Homodyne signal

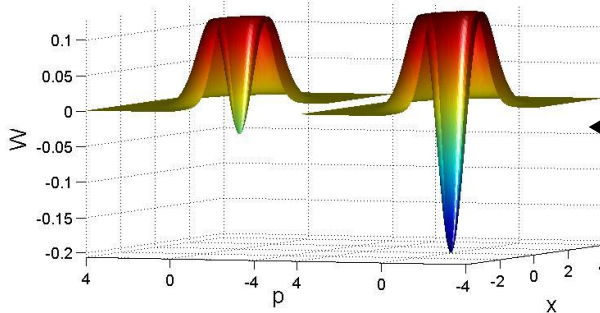


Quadrature distributions

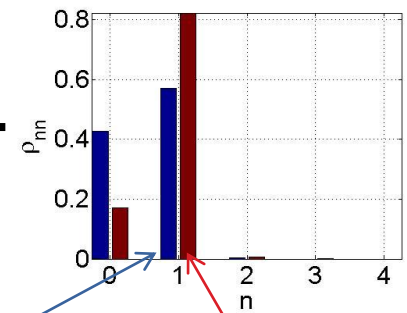


↓ maximal likelihood

Wigner function



Density matrix



measured state: 57%

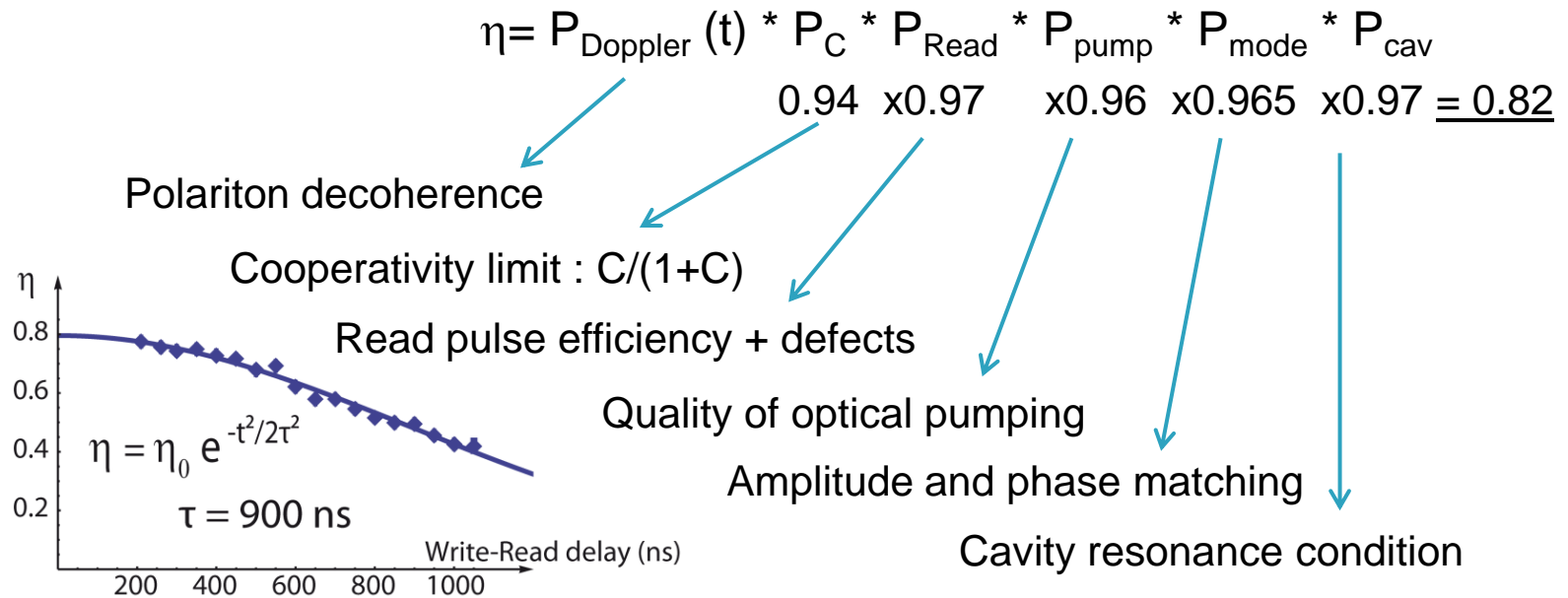
generated state: 82%



# Efficiency limits

Homodyne/counting measurements consistent:

- Temporal mode  $\exp(-t^2/2\tau^2)$ ,  $\tau=40\text{ns}$
- Generation efficiency  $\eta \sim 80\%$

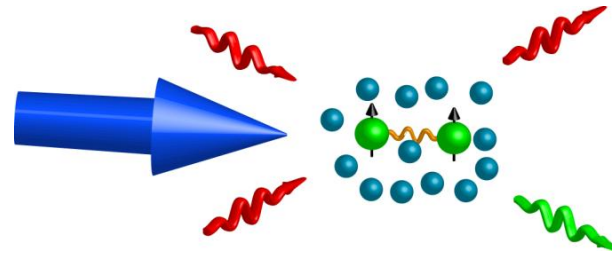


$\tau$  = Doppler decoherence time at  $50 \mu\text{K}$

# Outline

Atomic physics:  
create  
non-linear effects

**Part I**

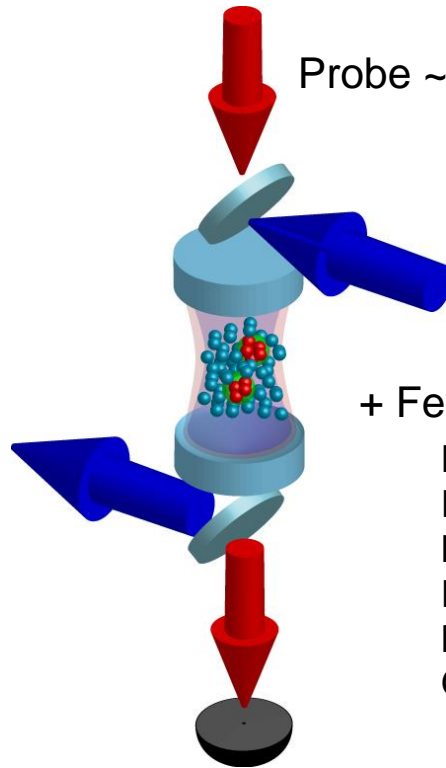


Quantum optics:  
Manipulate & detect  
quantum states

**Part II**

Rydberg-mediated  
photonic interactions  
**Part III**

# Quantum effects?



Probe  $\sim 1\text{nW}$   $\sim 1000$  photons  $\Rightarrow \sim 1$  photon?

+ Fewer losses than previous experiments?

Dudin & Kuzmich, *Science* **336**, 887 (2012),

Peyronel *et al*, *Nature* **488**, 57 (2012)

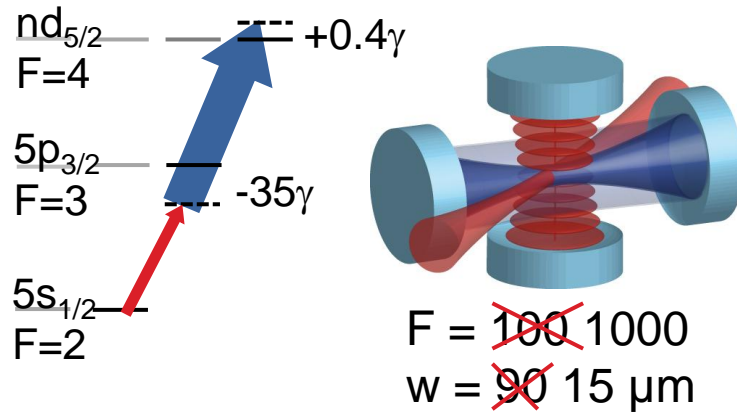
Maxwell *et al*, *PRL* **110**, 103001 (2013)

Firstenberg *et al*, *Nature* **502**, 71 (2013)

Baur *et al*, *PRL* **112**, 073901 (2014)

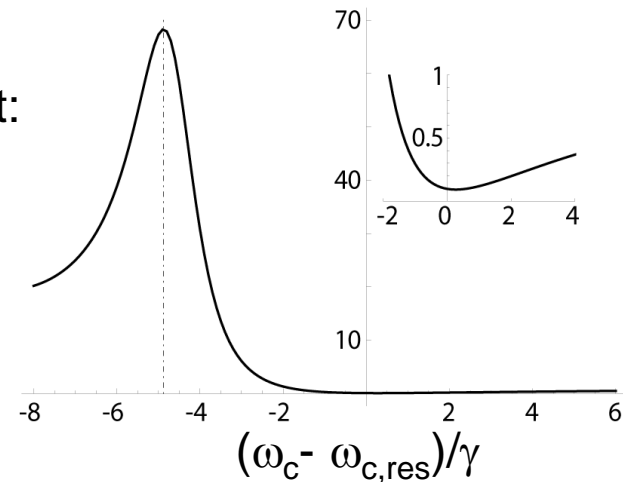
Gorniaczyk *et al*, *PRL* **113**, 053601 (2014)

# Off-resonant regime

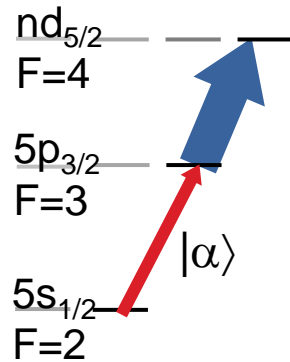


- ✓ Brighter, uniform control beam  
→ Buildup cavity ( $G \sim 16$ )
- ✓ Smaller, denser cloud  
→ Dipole trap ( $\sigma \sim 40 \mu\text{m}$ )
- ✗ Higher cavity finesse & smaller waist

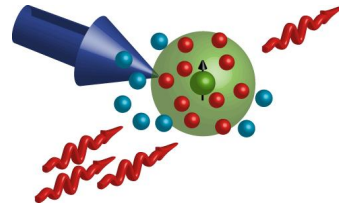
Expected  $g^{(2)}$  of transmitted light:  
(« Super-atom » model)



# Resonant regime



Free space:



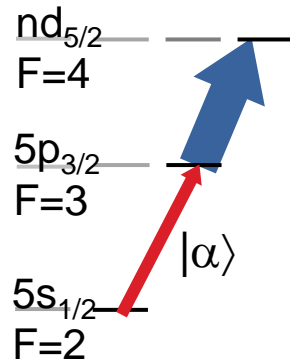
Non-linear losses  $\Rightarrow$  Single photon

Dudin & Kuzmich, *Science* **336**, 887 (2012),

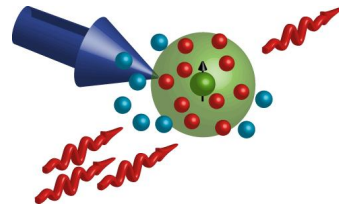
Peyronel *et al*, *Nature* **488**, 57 (2012)

Maxwell *et al*, *PRL* **110**, 103001 (2013)

# Resonant regime



Free space:



Non-linear losses  $\Rightarrow$  Single photon

Dudin & Kuzmich, *Science* **336**, 887 (2012),

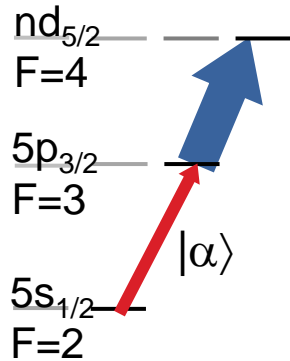
Peyronel *et al*, *Nature* **488**, 57 (2012)

Maxwell *et al*, *PRL* **110**, 103001 (2013)

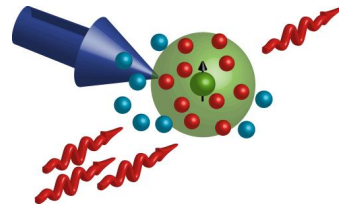
Cavity:

Turns losses into phase shift

# Resonant regime



Free space:



Non-linear losses  $\Rightarrow$  Single photon

Dudin & Kuzmich, *Science* **336**, 887 (2012),

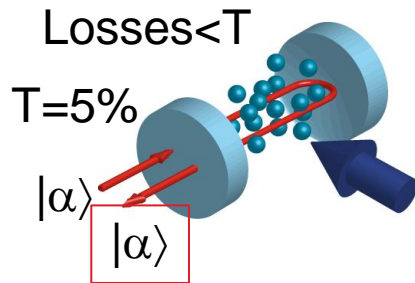
Peyronel *et al*, *Nature* **488**, 57 (2012)

Maxwell *et al*, *PRL* **110**, 103001 (2013)

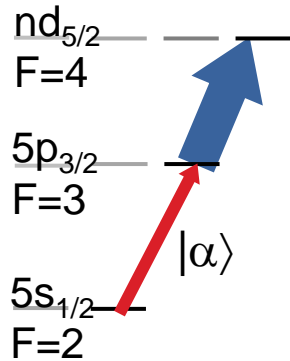
Cavity:

Turns losses into phase shift

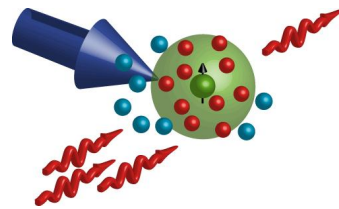
$|\alpha \ll 1\rangle$ : EIT



# Resonant regime



Free space:



Non-linear losses  $\Rightarrow$  Single photon

Dudin & Kuzmich, *Science* **336**, 887 (2012),

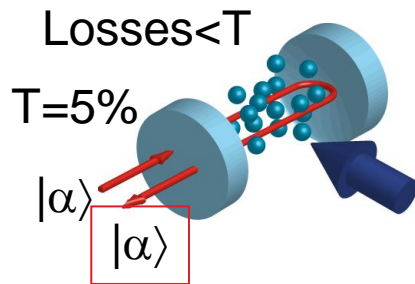
Peyronel *et al*, *Nature* **488**, 57 (2012)

Maxwell *et al*, *PRL* **110**, 103001 (2013)

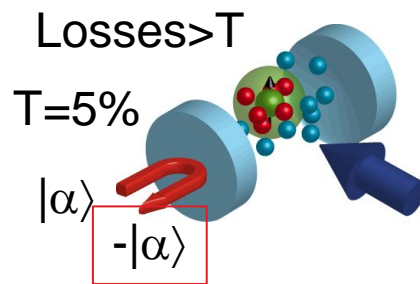
Cavity:

Turns losses into phase shift

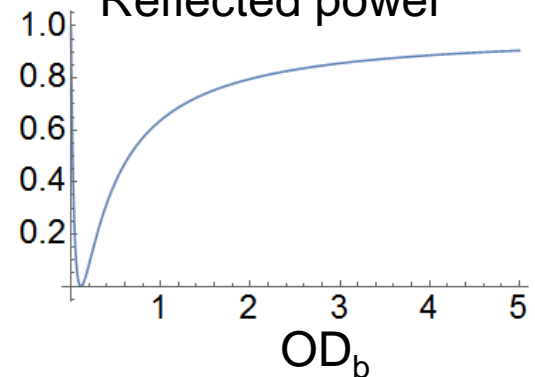
$|\alpha \ll 1\rangle$ : EIT



$|\alpha \gg 1\rangle$ : Blockade

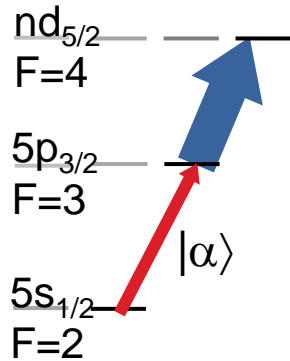


Reflected power

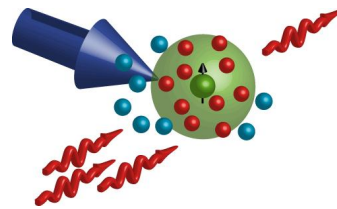




# Resonant regime



## Free space:



Non-linear losses  $\Rightarrow$  Single photon

Dudin & Kuzmich, *Science* **336**, 887 (2012),

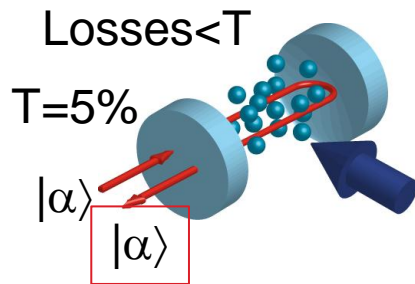
Peyronel *et al*, *Nature* **488**, 57 (2012)

Maxwell *et al*, *PRL* **110**, 103001 (2013)

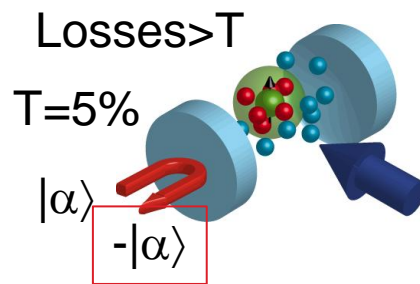
## Cavity:

Turns losses into phase shift

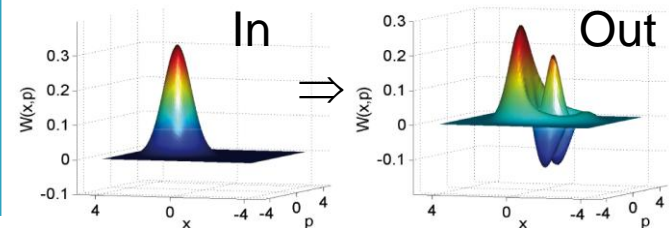
$|\alpha \ll 1\rangle$ : EIT



$|\alpha \gg 1\rangle$ : Blockade



$|\alpha \approx 1\rangle$ : Non-gaussian?



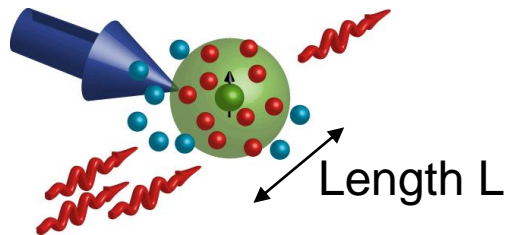
First experimental evidence of non-classical effects

# No free lunch

- Additional technical complexity (OK)
- Specific theoretical models (OK)
- Temporal/spectral issues :

Can the tail of a photon enter the system before its head comes out?

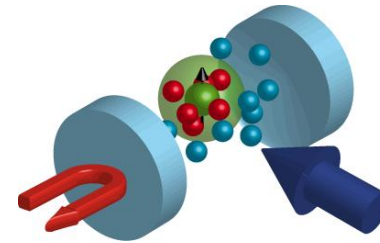
Free space:



Time to cross the gas  $\propto L$   
EIT linewidth  $\propto L^{-1/2}$

$\Rightarrow$  OK

Cavity:

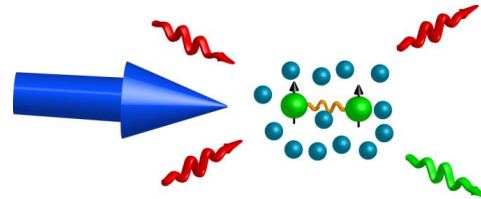


Storage time  $\propto (\text{linewidth})^{-1} \dots$

Dynamic control  $\Rightarrow$  OK

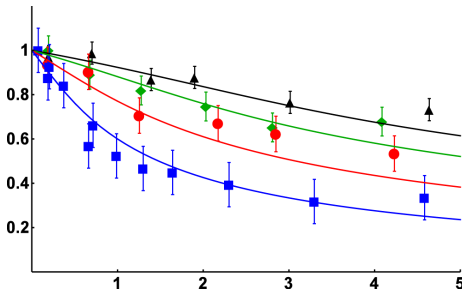
# Conclusion

Rydberg physics:  
create  
non-linear effects



Quantum optics:  
Manipulate & detect  
quantum states

PRA **88**, 053845 (2013)  
PRL **109**, 233602 (2012)

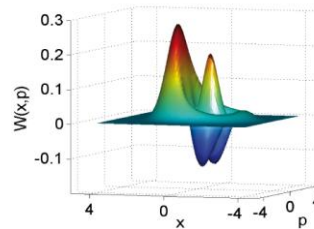
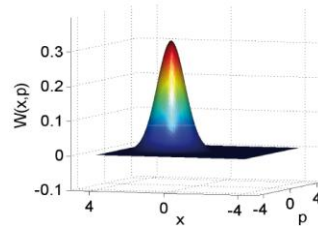
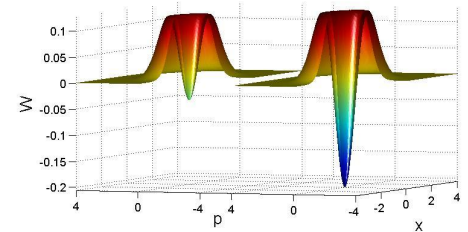


Rydberg-mediated  
photonic interactions

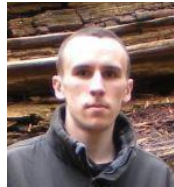
PRA **86**, 021403(R) (2012)  
NJP **16**, 043020 (2014)

Work in progress

PRA **84**, 053830 (2011)  
PRL **112**, 033601 (2014)



# Thanks!



Erwan  
Bimbard



Rajiv  
Boddeda



Andrey  
Grankin



Nicolas  
Vitrant



Valentina  
Parigi



Jovica  
Stanojevic



Imam  
Usmani



Philippe  
Grangier

+ Etienne Brion & Pierre Pillet  
(LAC Orsay)



European  
Research  
Council

# Thanks!



Durham  
University

Charles  
Adams

Dr. Erwan Bimbard Rajiv Boddeda Andrey Grankin Nicolas Vitrant



Valentina Parigi Jovica Stanojevic Imam Usmani Philippe Grangier

+ Etienne Brion & Pierre Pillet  
(LAC Orsay)



European  
Research  
Council

# Thanks!



**Dr.** Erwan Bimbard    Rajiv Boddeda    Andrey Grankin    Nicolas Vitrant



Valentina Parigi    Jovica Stanojevic    Imam Usmani    Philippe Grangier

+ Etienne Brion & Pierre Pillet  
(LAC Orsay)



European  
Research  
Council

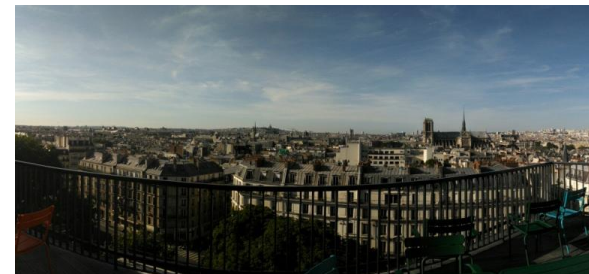


Durham  
University

Charles  
Adams

A.O. (+Post-doc: Kilian Müller)

COLLÈGE  
DE FRANCE  
— 1530 —



Looking for PhD students!